

MOLSSI WORKSHOP – ELSI CONFERENCE:
“SOLVING OR CIRCUMVENTING EIGENVALUE PROBLEMS IN
ELECTRONIC STRUCTURE THEORY”
RICHMOND, VIRGINIA – 26TH AUGUST 2018

Recent Advancements in ELPA: Best Practices in Real Applications

Danilo Simoes Brambila and Christian Carbogno



FRITZ-HABER-INSTITUT
DER MAX-PLANCK-GESELLSCHAFT,
BERLIN - GERMANY

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Code Testing,
Benchmarking,
and Validation
in *Real*
Applications

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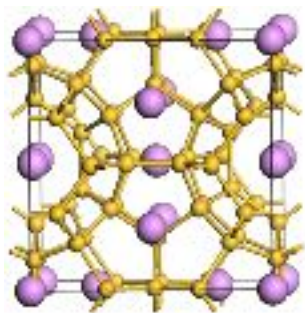
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Electronic Structure Theory
Density Functional Theory



**Solid State Physics &
Material Science**

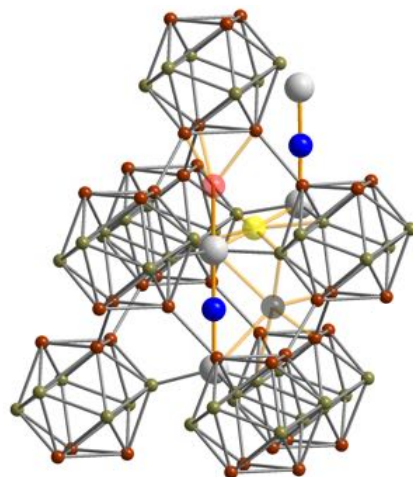


***Thermoelectric
Clathrates***

A. Bhattacharya, *et al.*,
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***Thermoelectric
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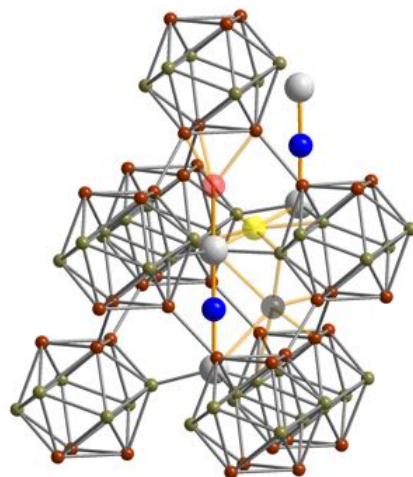


**Thermoelectric
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**Functional
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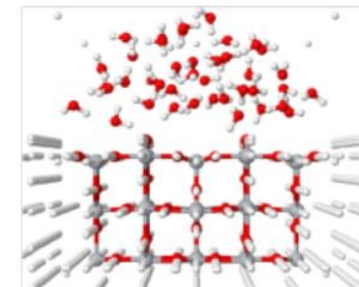
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Quantum Chemistry

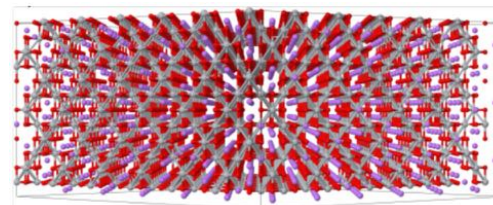
**Free Energy Barriers
for H_2O on TiO_2**

T. Stecher, *et al.*,
Phys. Rev. Lett. **117**, 276001 (2017).



**Occupations Disorder
in $Li_4Ti_5O_{12}$ Batteries**

H. Heenen *et al.*,
Nano Letters **17**, 3884 (2017).



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**Christoph
Scheurer**

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Algorithmic
Developments
&
Advancements



BERGISCHE
UNIVERSITÄT
WUPPERTAL



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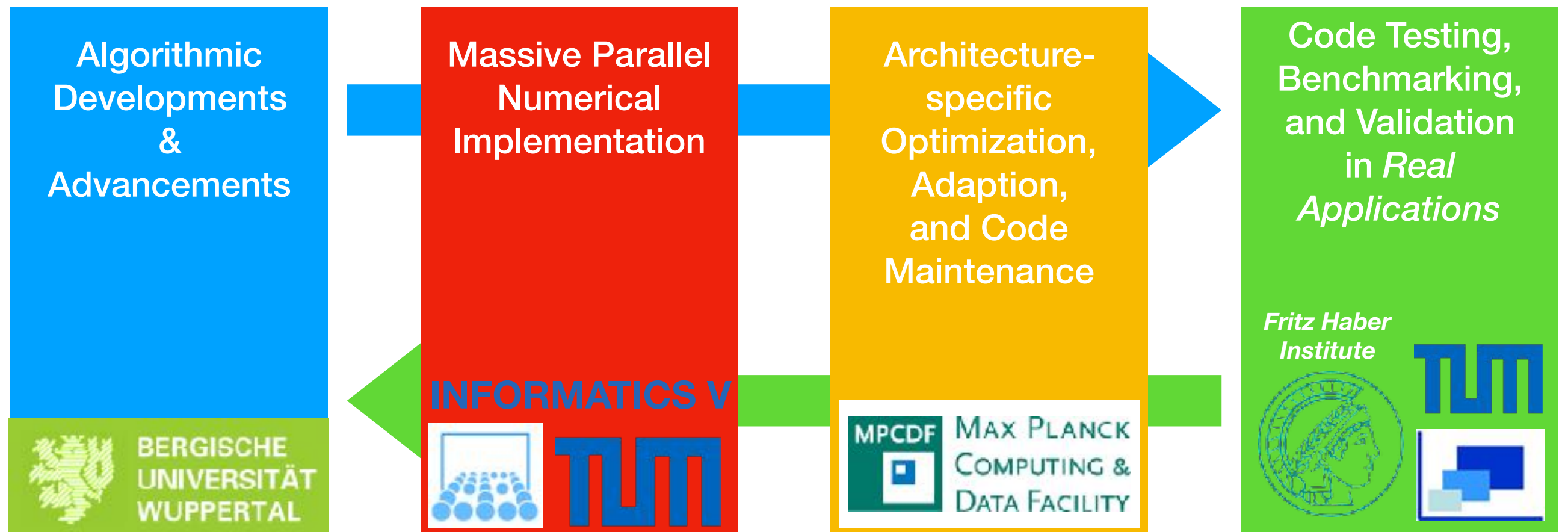
TUM



Bruno Lang

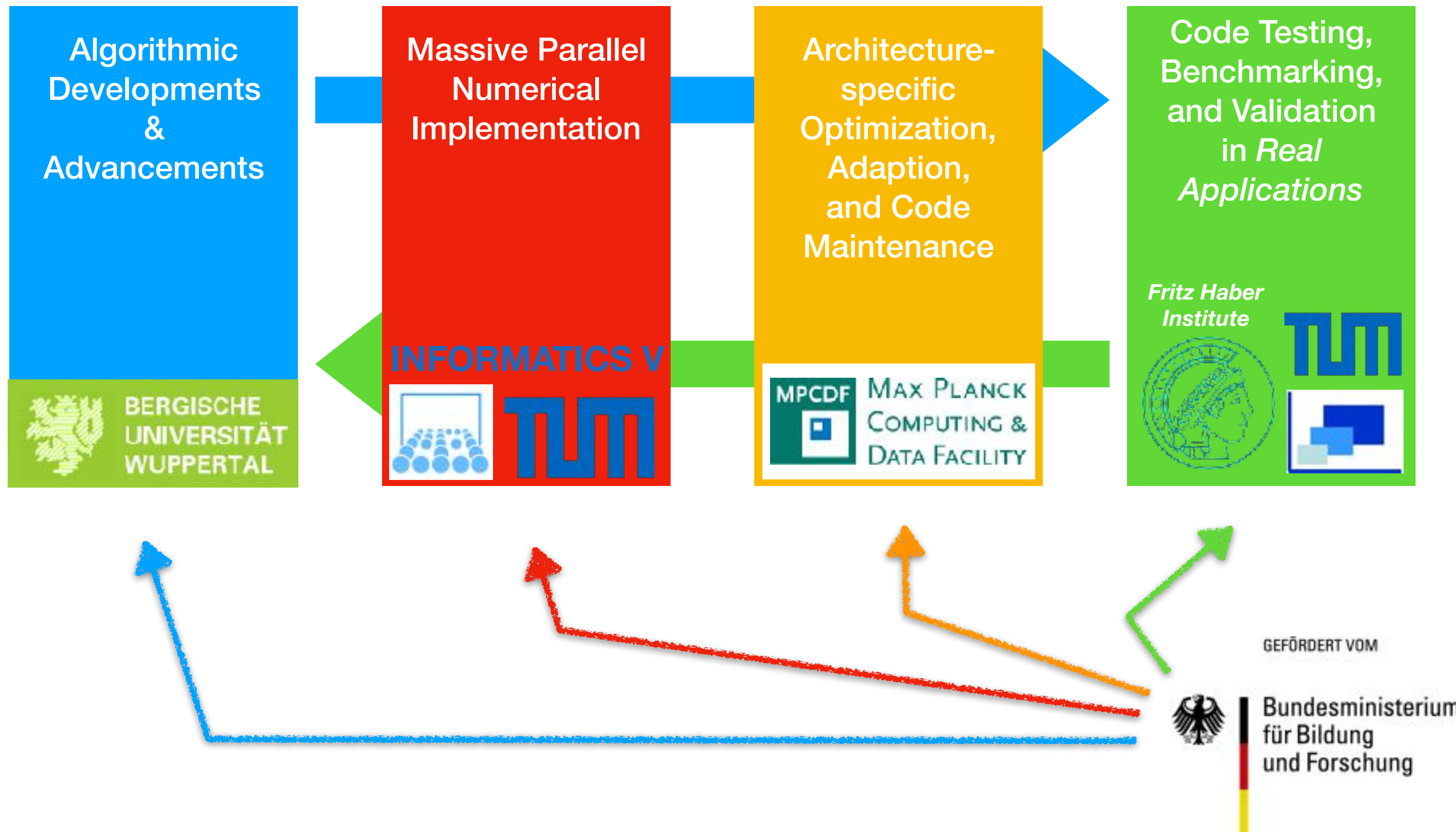
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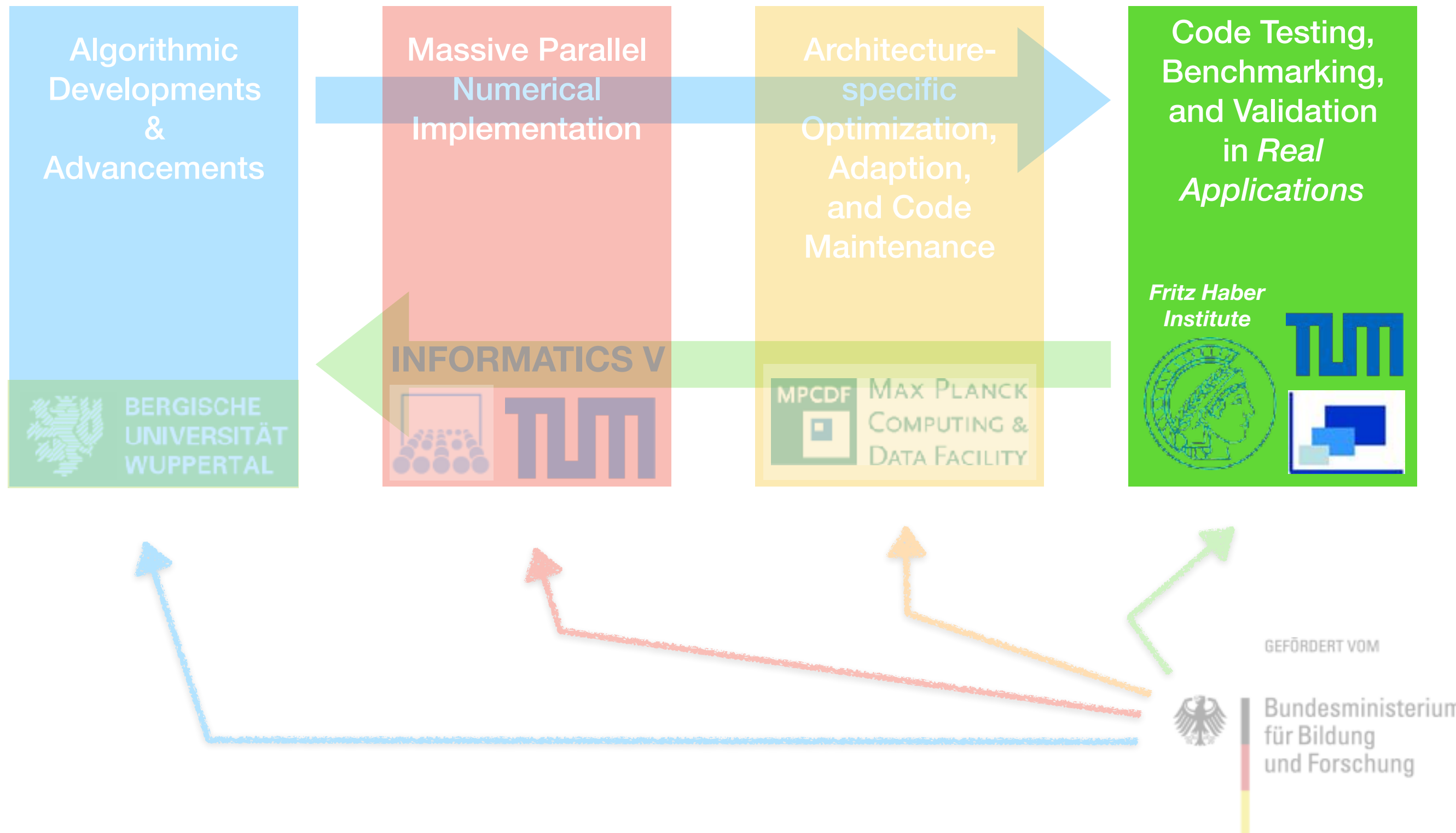
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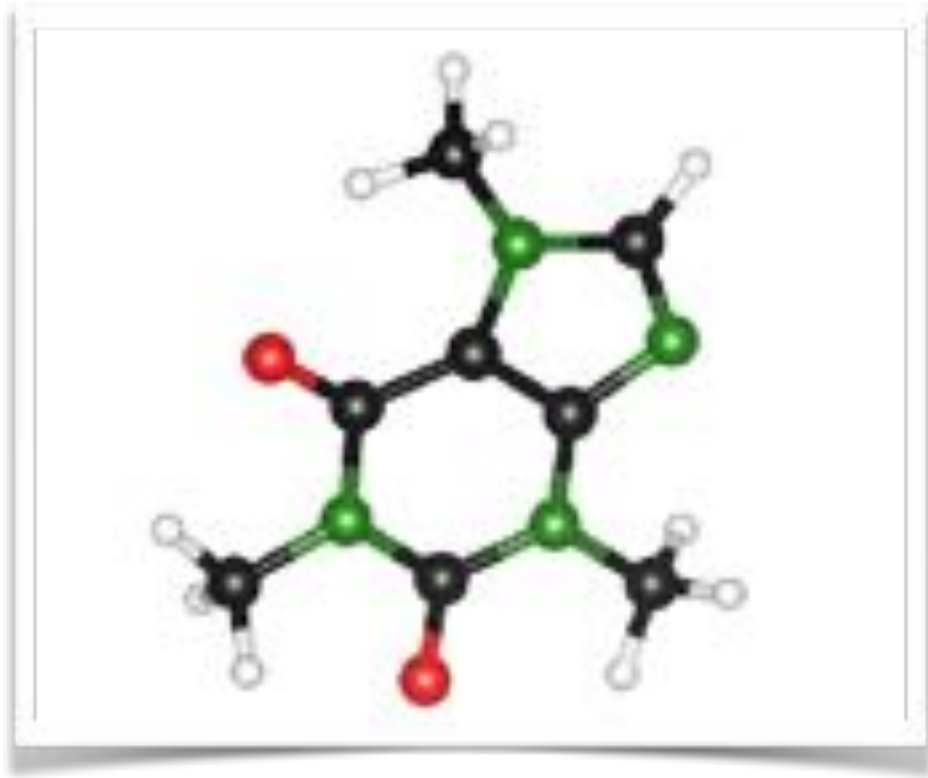


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Electronic Structure Theory 101

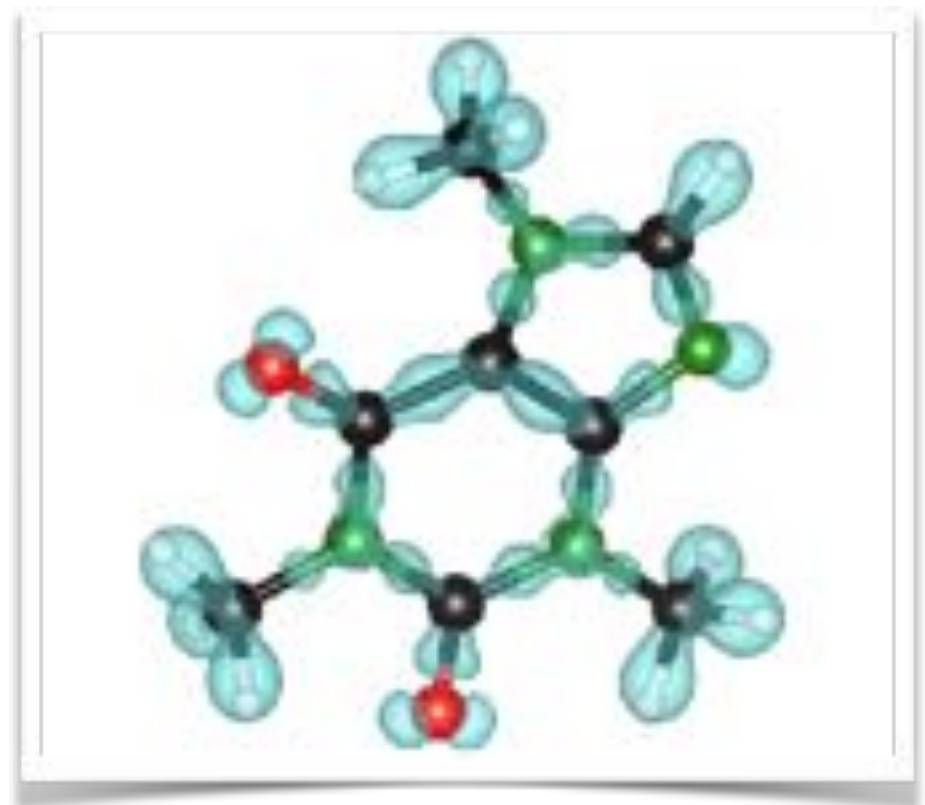
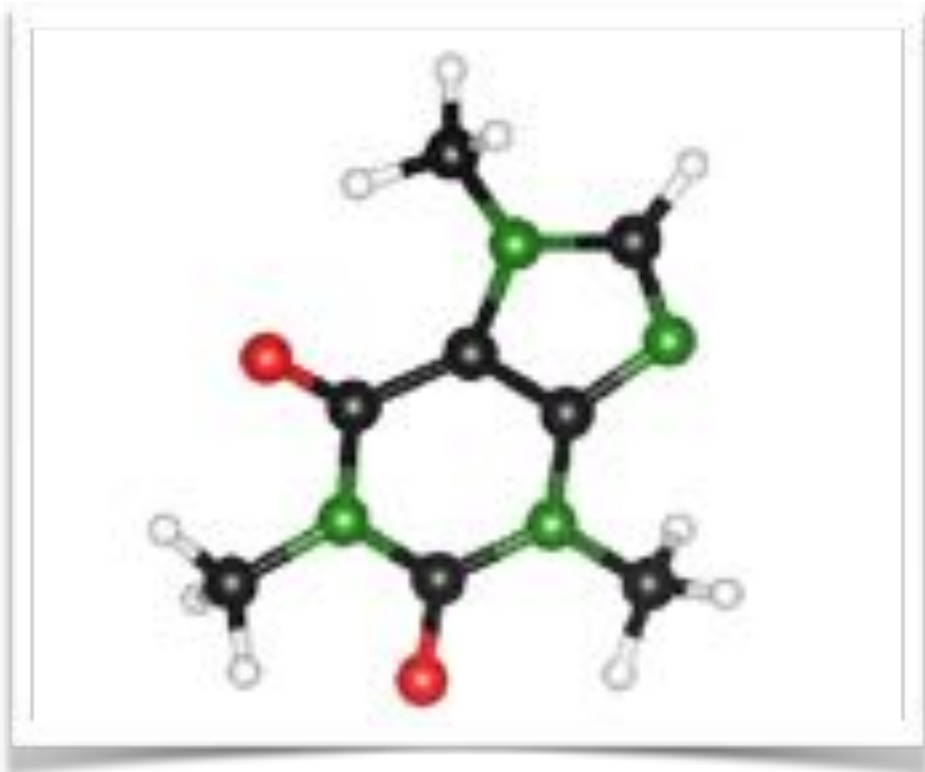


INPUT

M three-dimensional vectors \mathbf{R}_I defining the **position** of the individual nuclei I in space

M values Z_I for the charge defining the **chemical species** of the nuclei I

Electronic Structure Theory 101



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Electronic Structure Theory

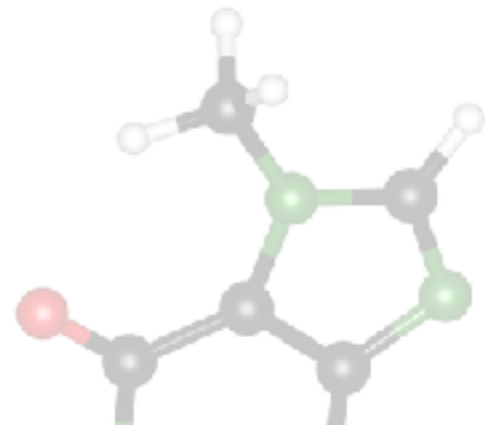
OUTPUT

Spatial distribution of N electrons, e.g., the *electronic density* $n(\mathbf{r})$ with

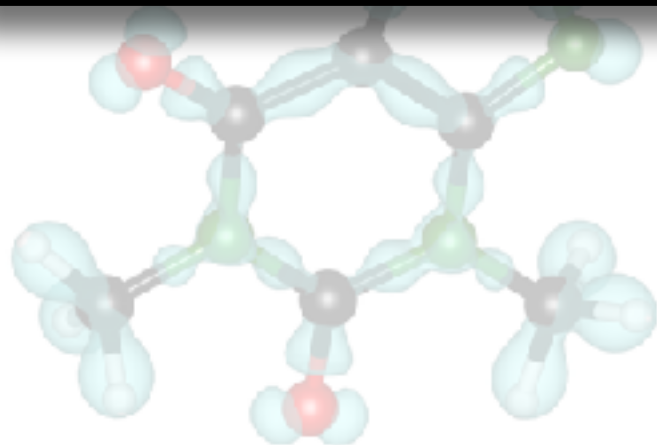
$$N = \int n(\mathbf{r}) d\mathbf{r}$$

in ***density-functional theory*** (1998 Nobel Prize).

Electronic Structure Theory 101



*Eigenvalue
Problem
Computationally
Dominant!*



INPUT

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Electronic Structure Theory

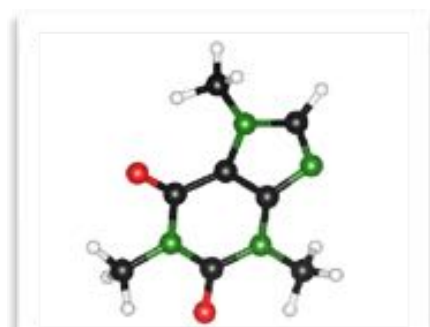
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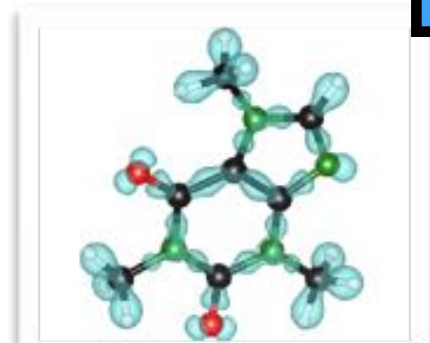
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Electronic Structure Theory 101



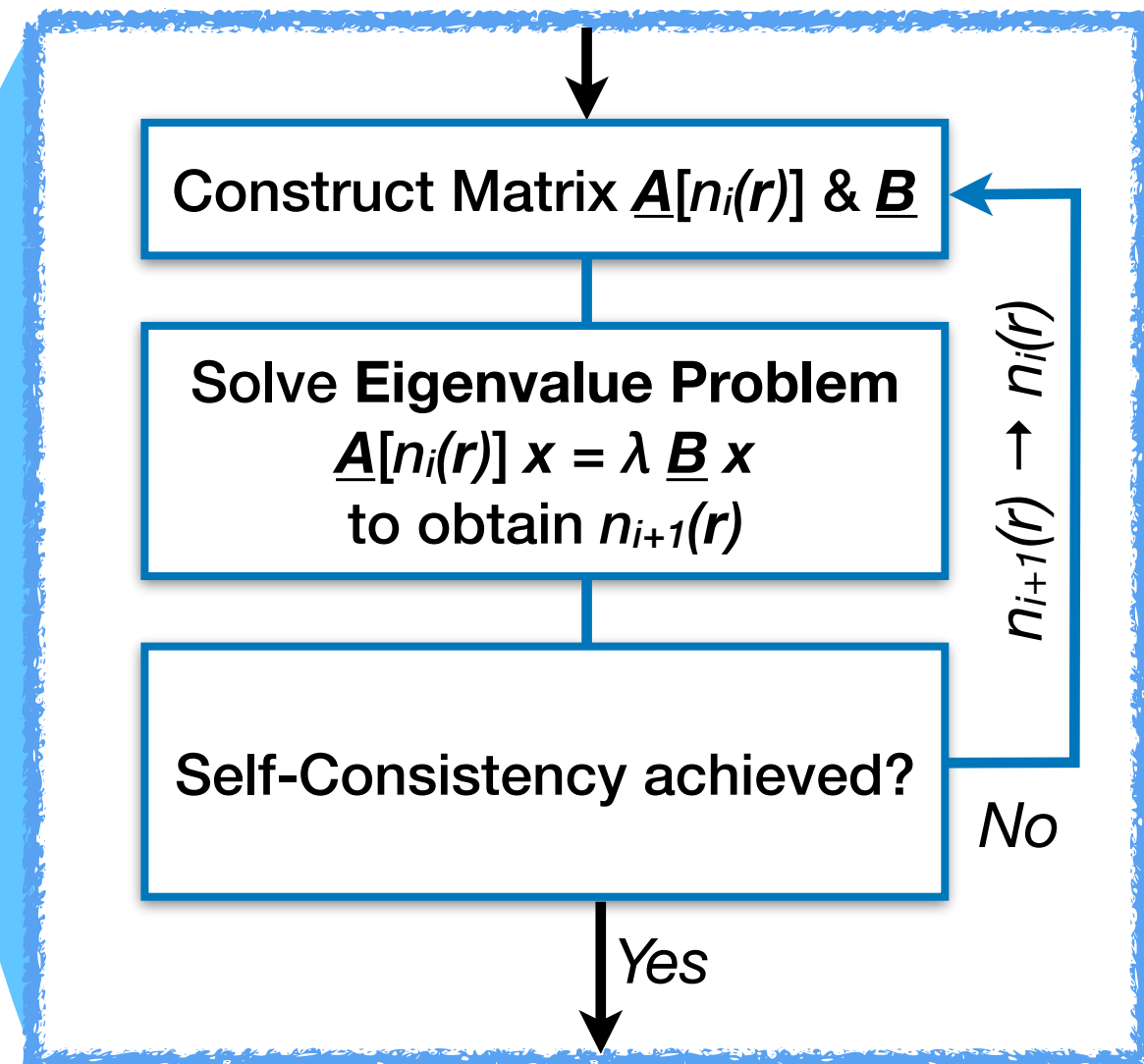
Geometry & Species



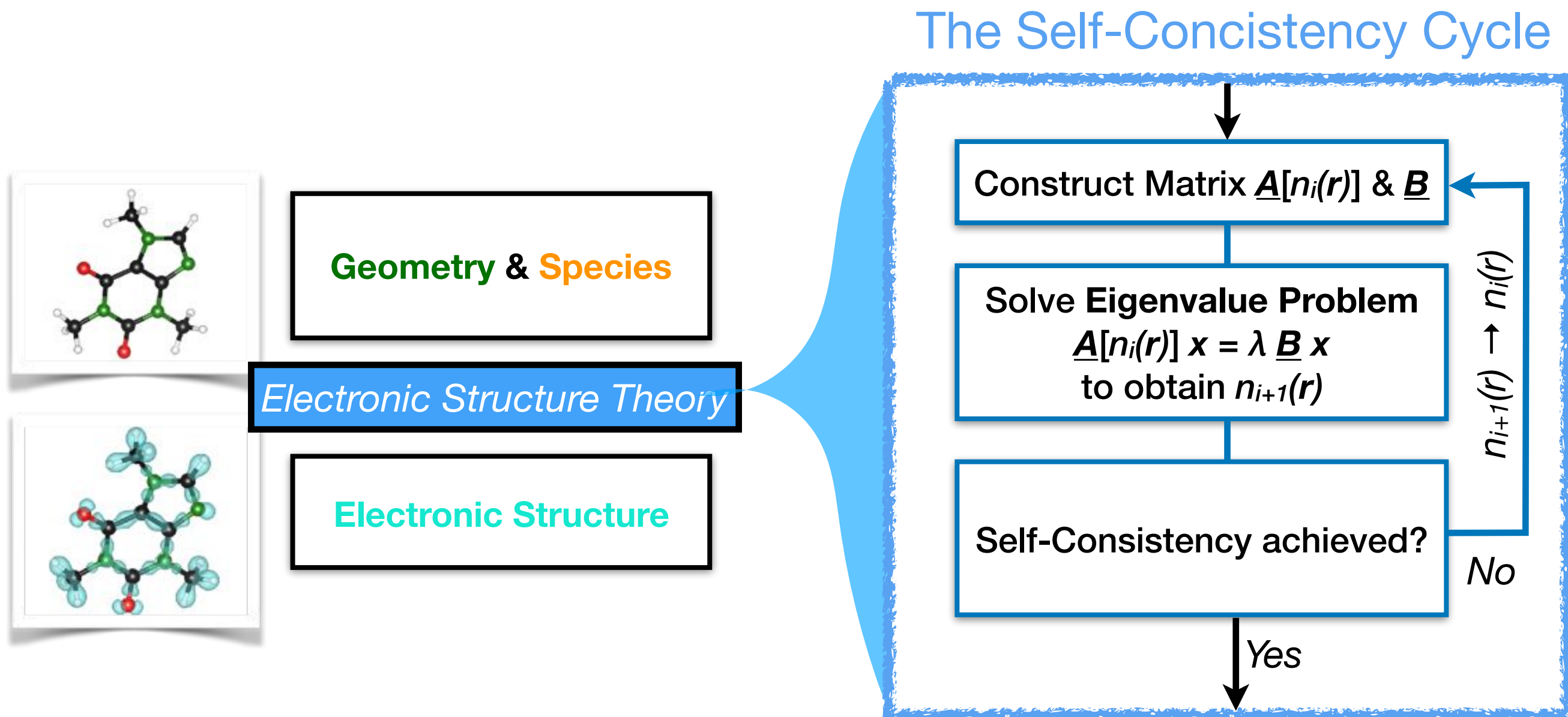
Electronic Structure Theory

Electronic Structure

The Self-Consistency Cycle



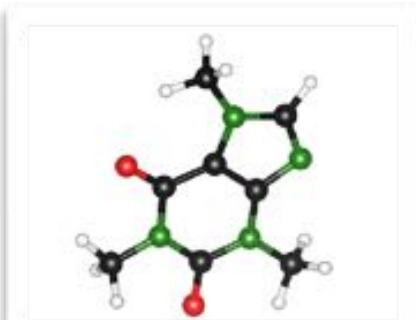
Electronic Structure Theory 101



A series of different eigenproblems
with *same* \underline{B} are solved one after another.

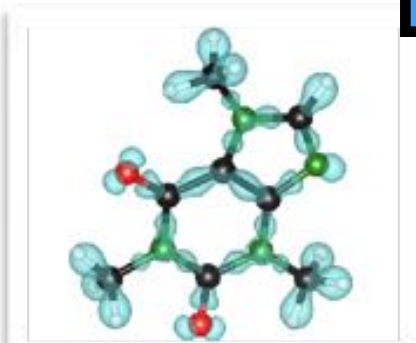
Electronic Structure Theory 101

Update Geometry



Geometry & Species

Electronic Structure Theory



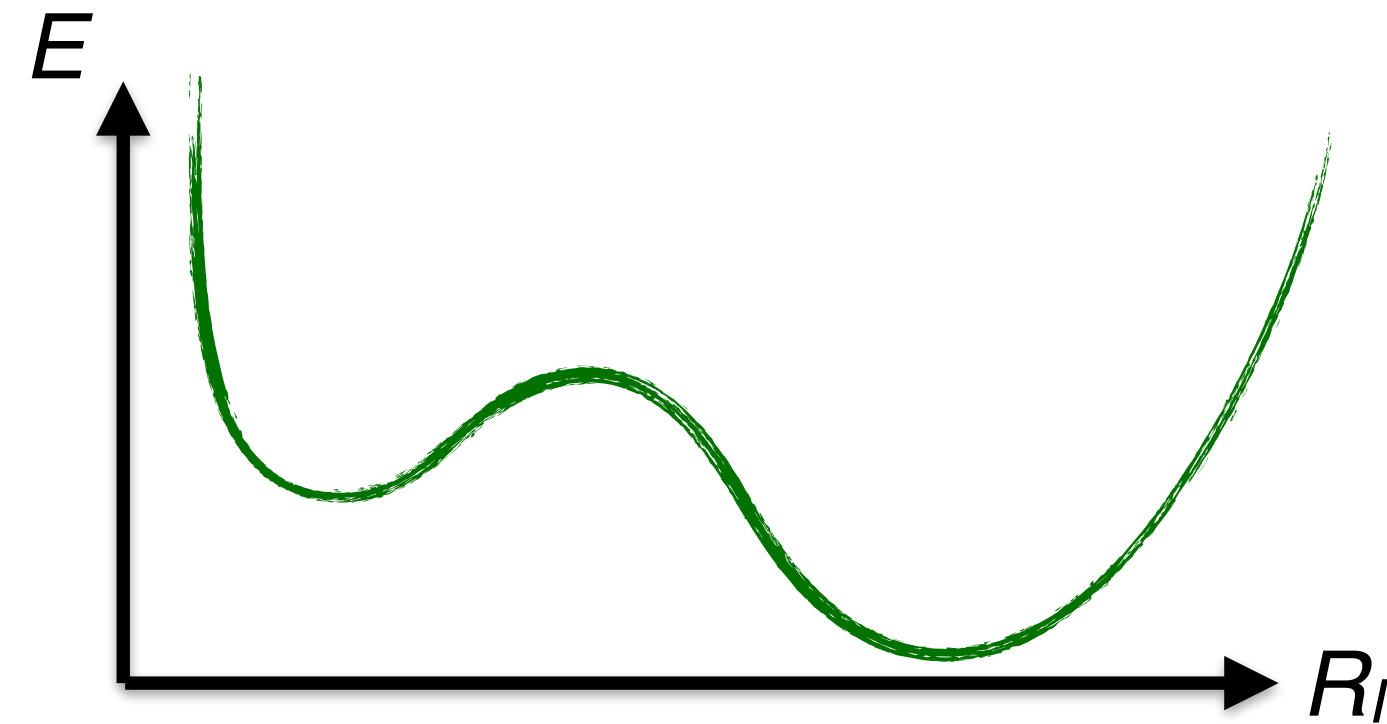
Electronic Structure

**Compute Energy E
and Forces F on Atoms**

⇒ Materials' Properties

**A series of different,
but similar electronic
structure theory
problems are solved
one after another.**

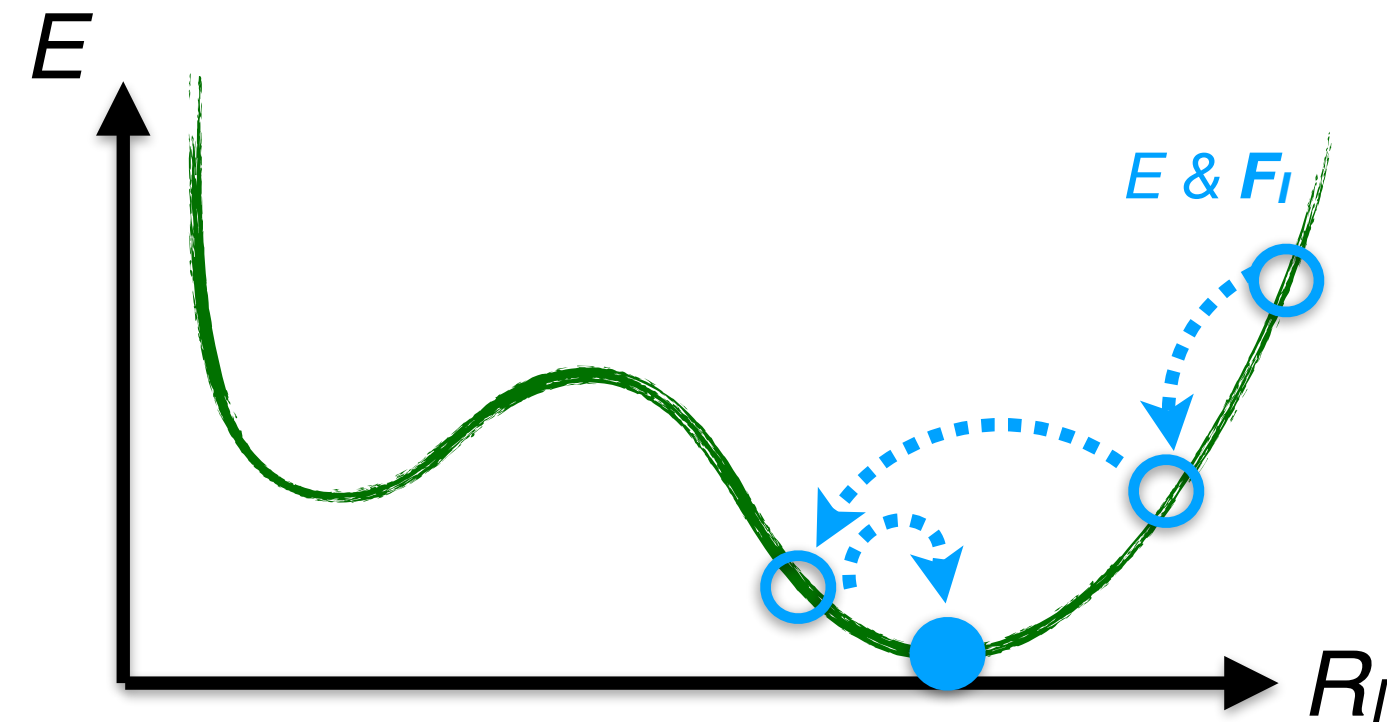
Exploring the Potential-Energy Surface



The *Potential-Energy Surface (PES)* describes the **dependence** of the **energy E** on the M **nuclear positions R_l** .

The *Potential-Energy Surface (PES)* determines the **dynamics** of the **nuclei**.

Exploring the Potential-Energy Surface

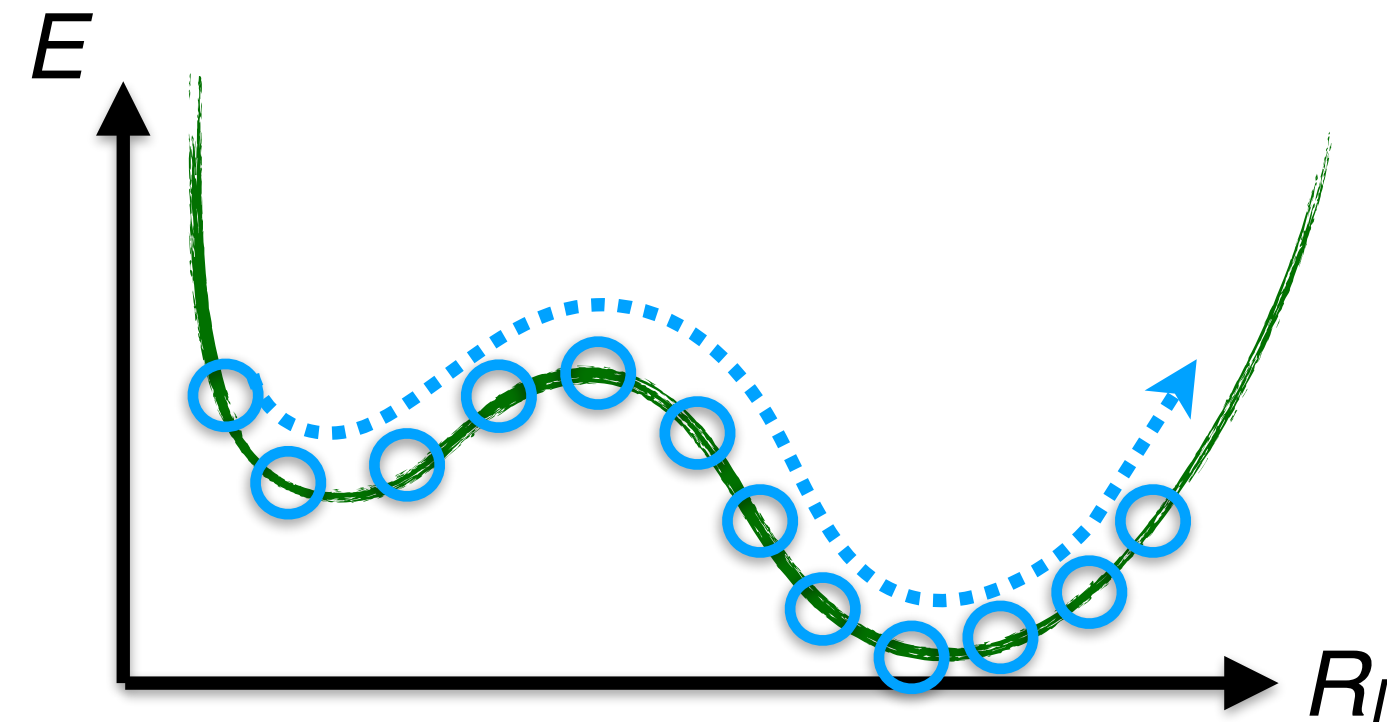


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- **Iterative Minimization (“Relaxation”)**: Find the *minima* of the PES
⇒ Most probable configuration(s), static properties, stabilities,...

Exploring the Potential-Energy Surface

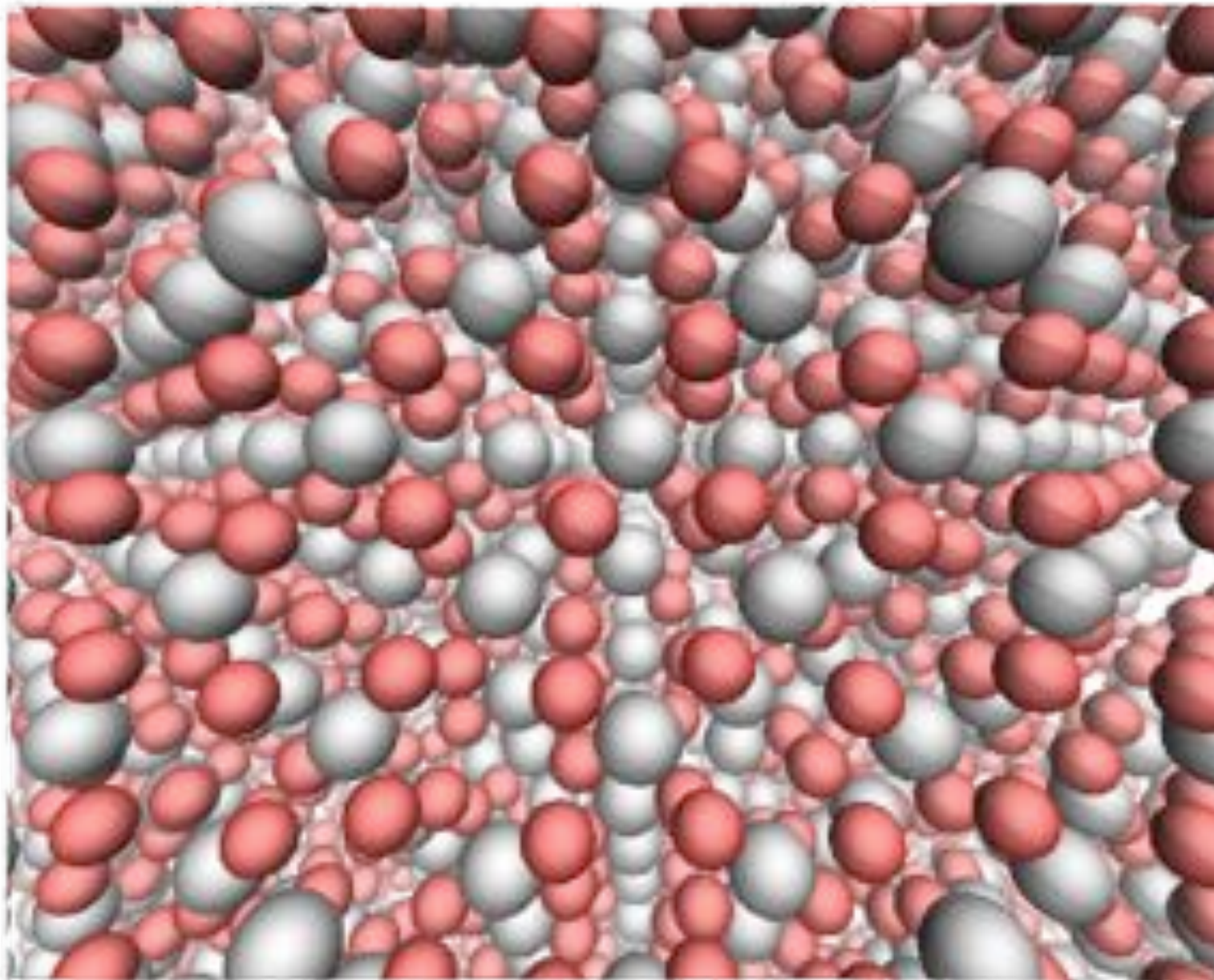
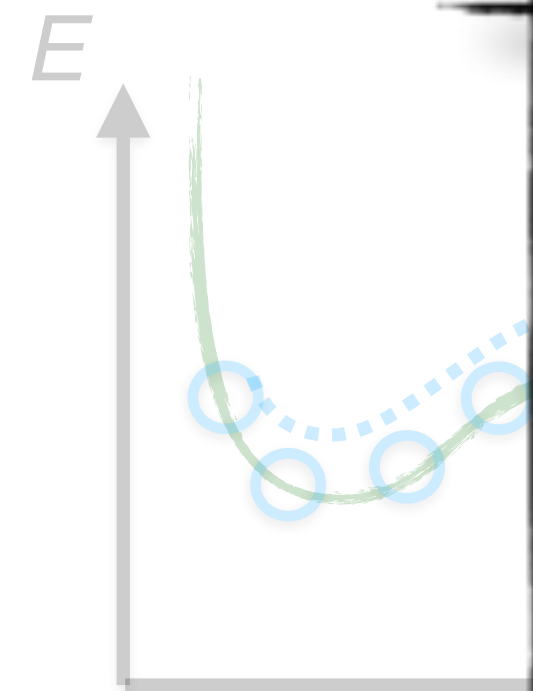


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- **Iterative Minimization (“Relaxation”)**: Find the *minima* of the PES
- ***Ab initio* Molecular Dynamics**: Iteratively integrate the equations of motion
⇒ **Quantitative explore the full Dynamics!**

Exploring the Potential-Energy Surface



- Iterative Minimization
- Transition-State Theory
- *Ab initio* Molecular Dynamics

⇒ Quantitative explore the full Dynamics!

• Surface (PES)
dependence of the
nuclear positions R_i .

• Surface (PES)
dynamics of the nuclei.

• Minima of the PES

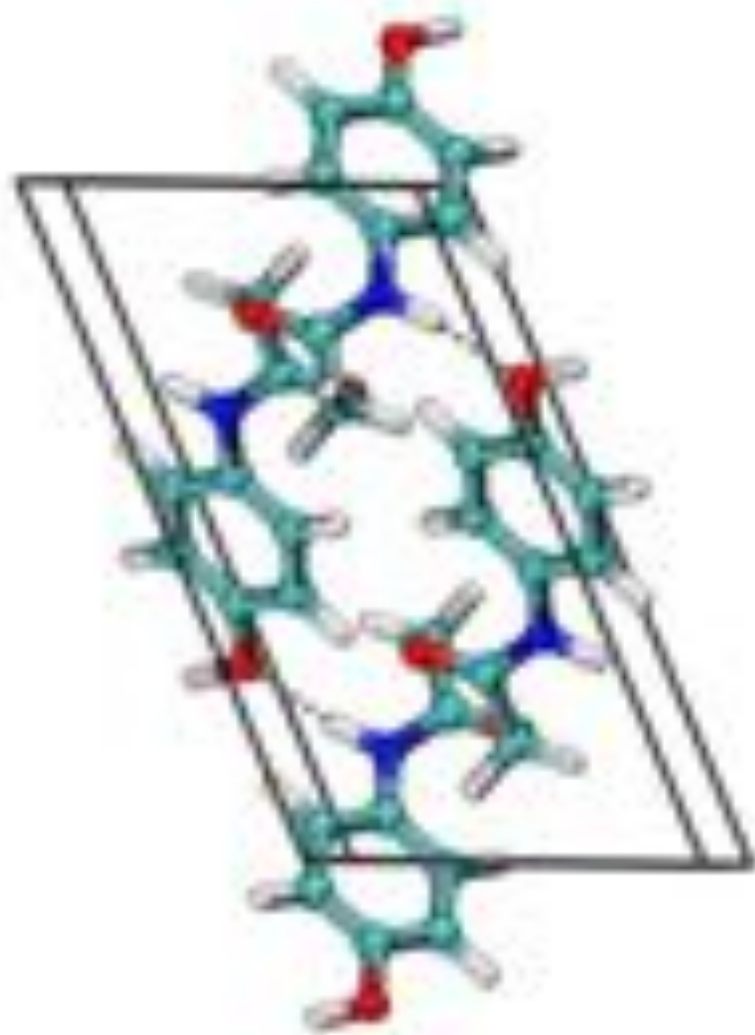
• Motion

Example A: Paracetamol

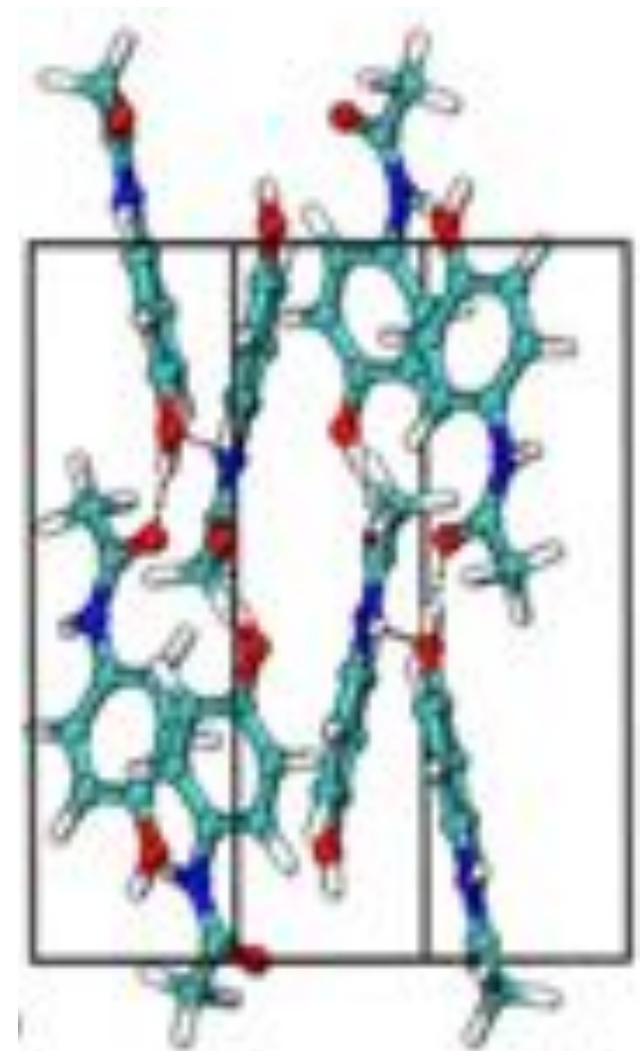
H. Shang, et al., New J. Phys., **DOI:** [10.1088/1367-2630/aace6d](https://doi.org/10.1088/1367-2630/aace6d)

Paracetamol exists in two different polymorphs:
“Same paracetamol molecules, different crystalline order”

Form I:



Form II:

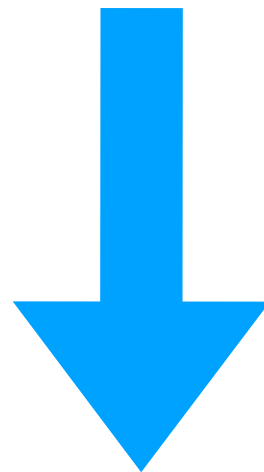
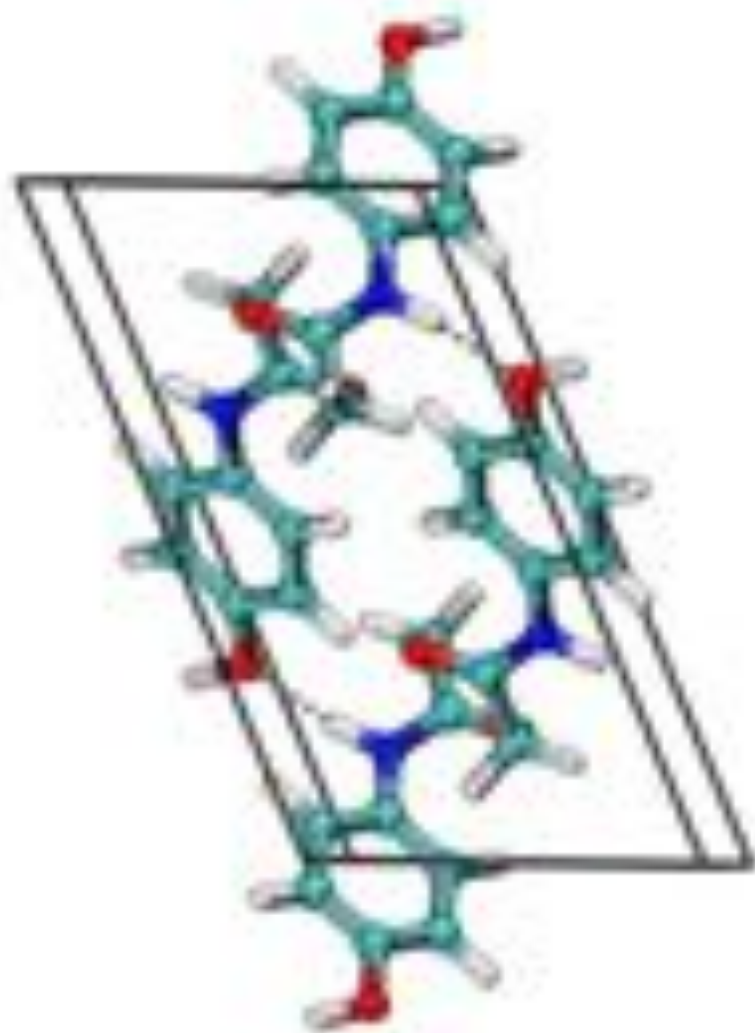


Example A: Paracetamol

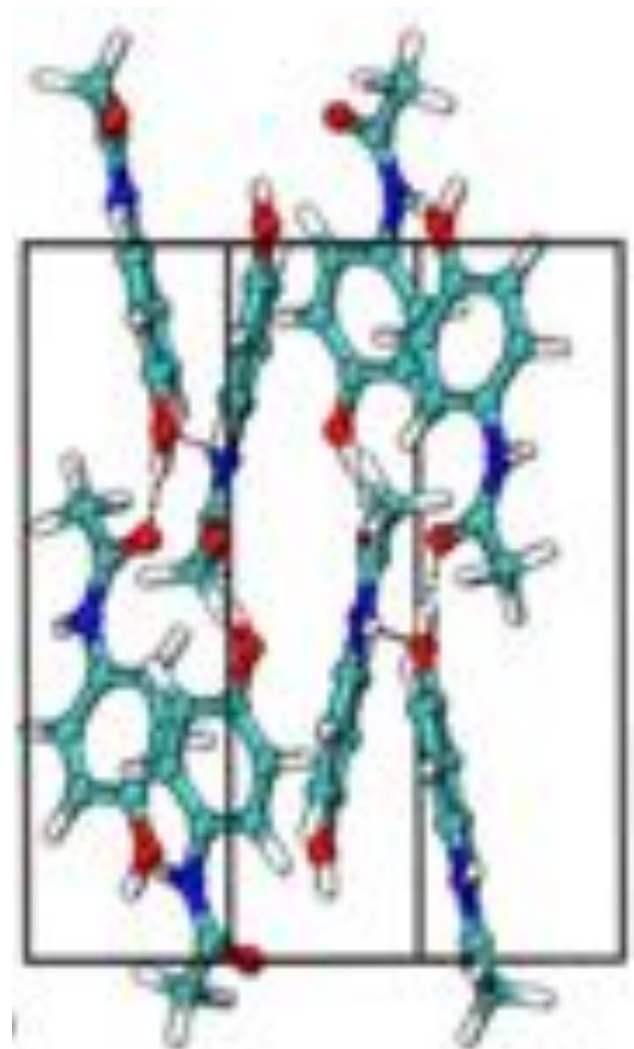
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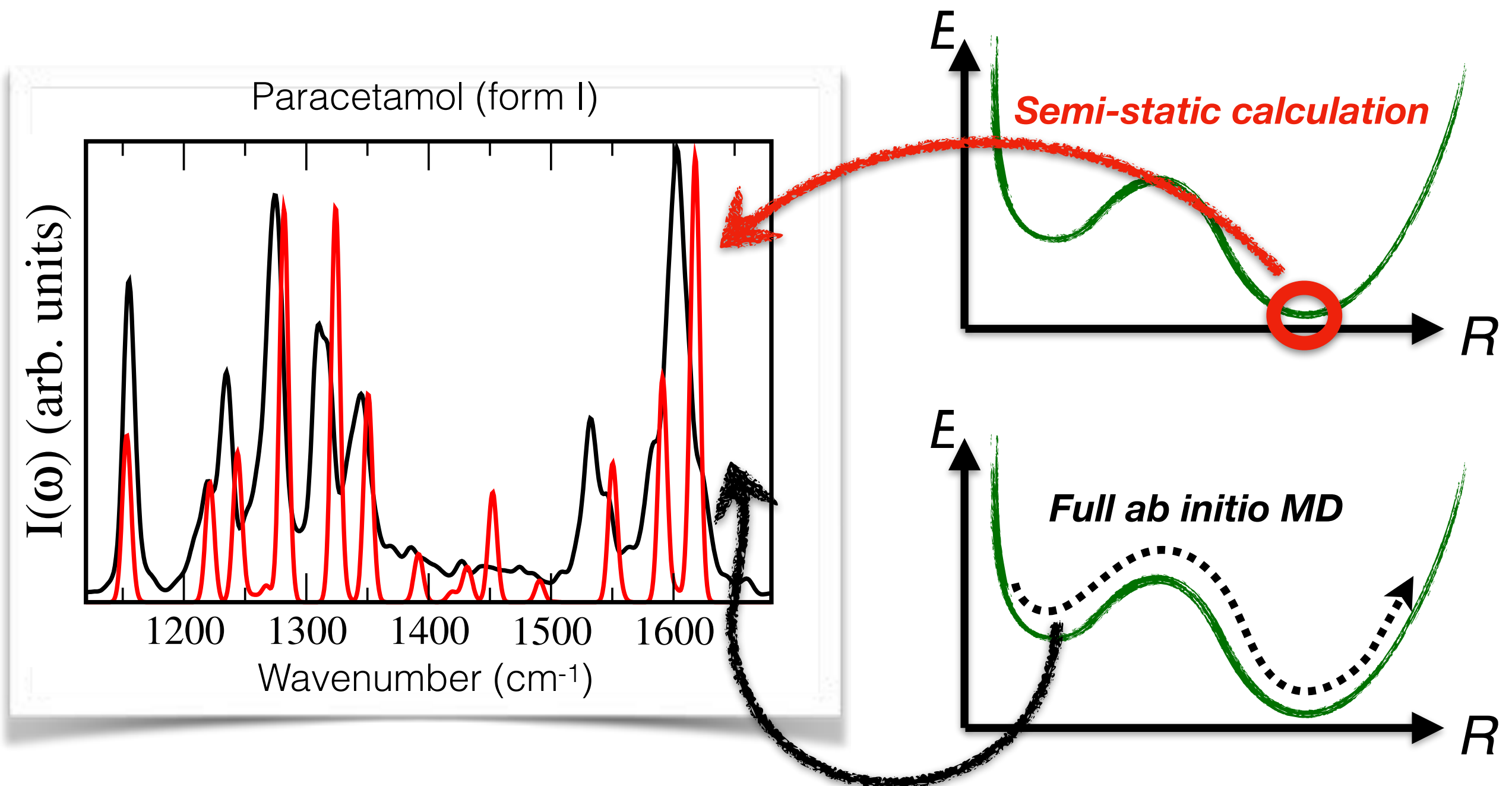


The two forms differ in
their physico-chemical
properties, e.g.,
solubility.

Example A: Paracetamol

*H. Shang, et al., New J. Phys. **20**, 073040 (2018).*

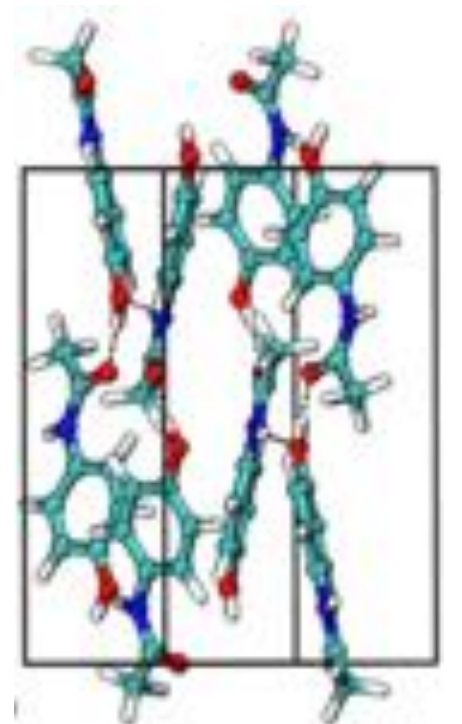
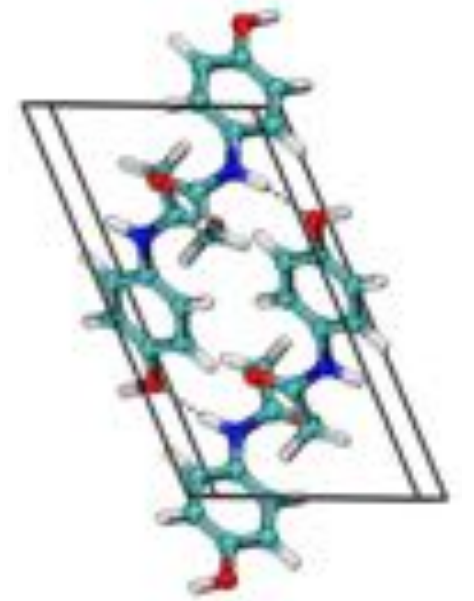
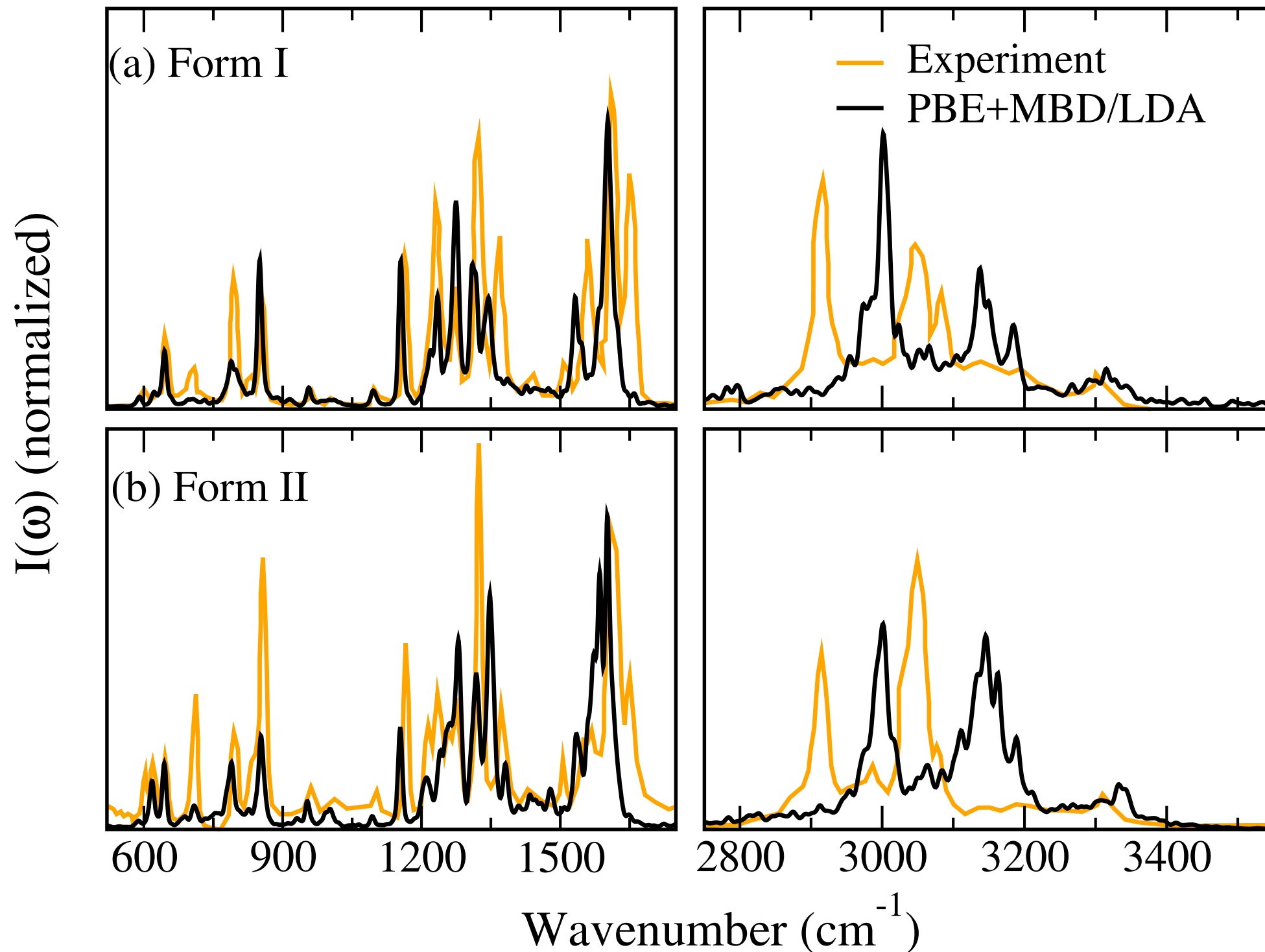
Raman Spectra describing the response to **electric fields** typically used to differentiate between **two polymorphs**.



Example A: Paracetamol

*H. Shang, et al., New J. Physics, **20**, 073040 (2018).*

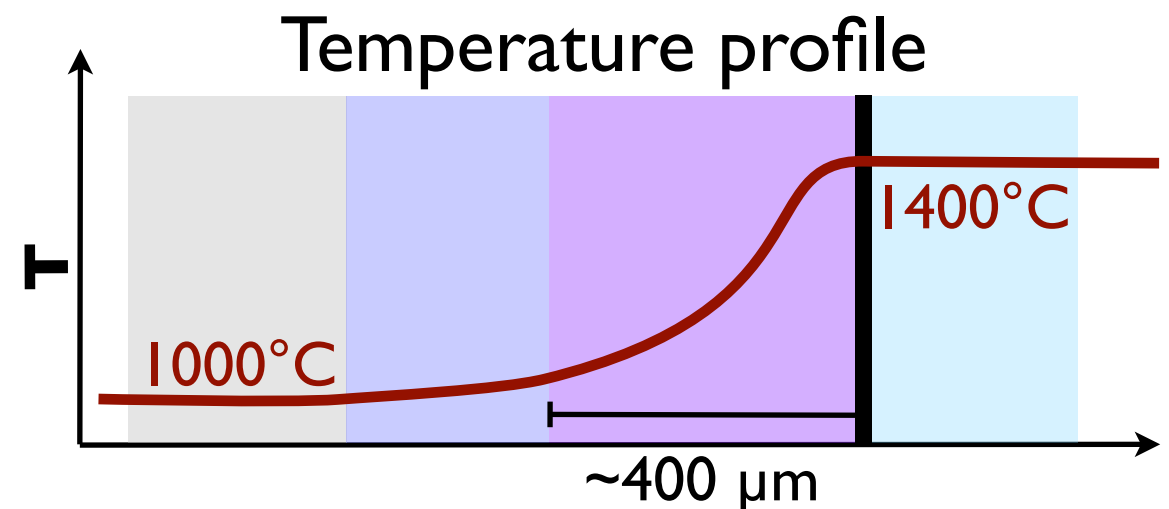
Exp.: J. B. Nanubolu and J. C. Burley. *Mol. Pharm.*, **9**, 1544 (2012).



Example B: Thermal-Barrier Coatings



CFM 56-7 airplane engine

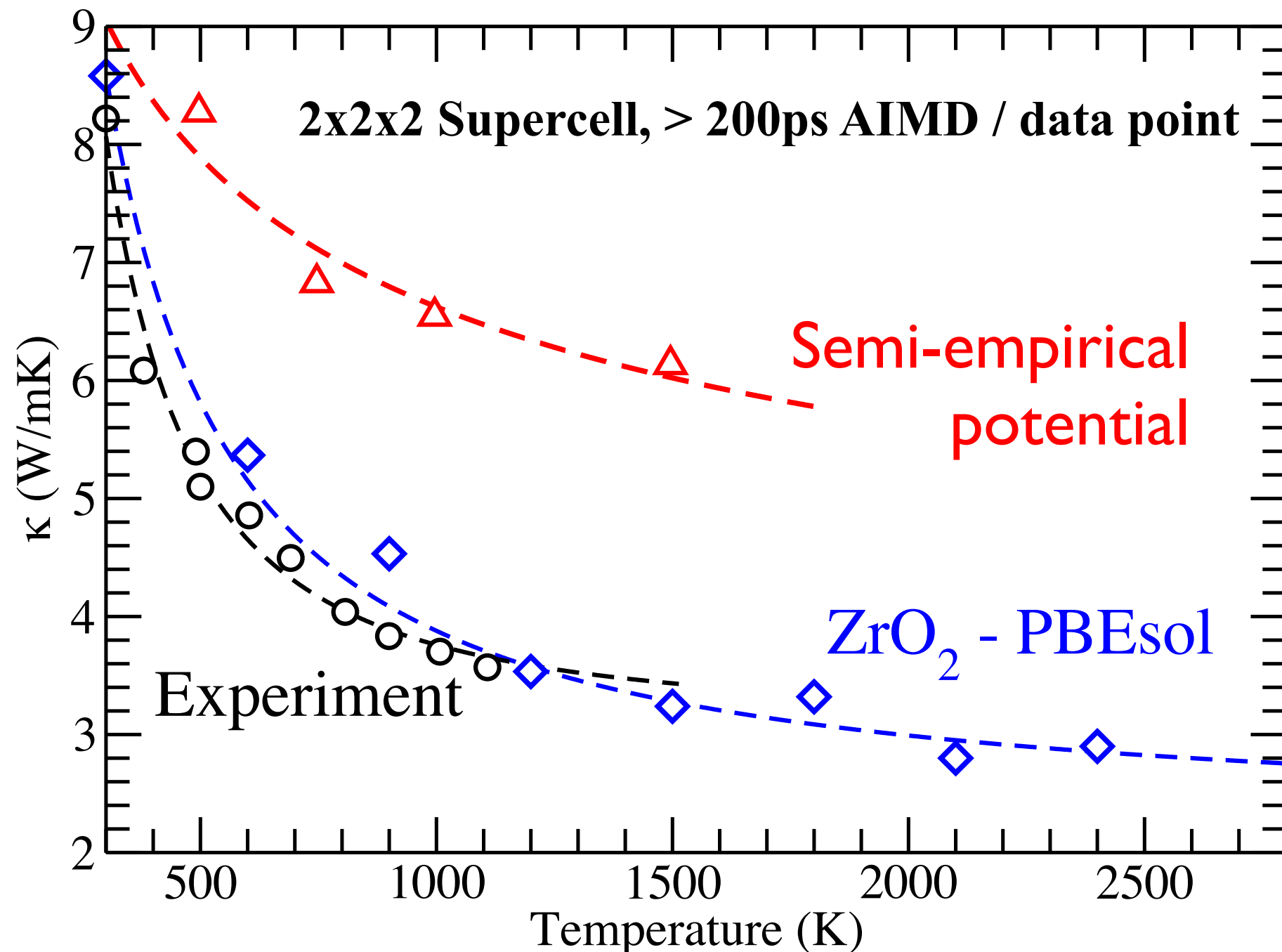


Suppressing heat transport in **thermal barrier coatings** has driven the fuel-efficiency increase over the last 30 years.

D. R. Clarke & C. G. Levi, *Ann. Rev. Mat. Res.*, **33**, 383 (2003).

THERMAL CONDUCTIVITY OF ZIRCONIA

C. Carbogno, R. Ramprasad, and M. Scheffler, *Phys. Rev. Lett.* **118**, 175901 (2017).



Experiment:

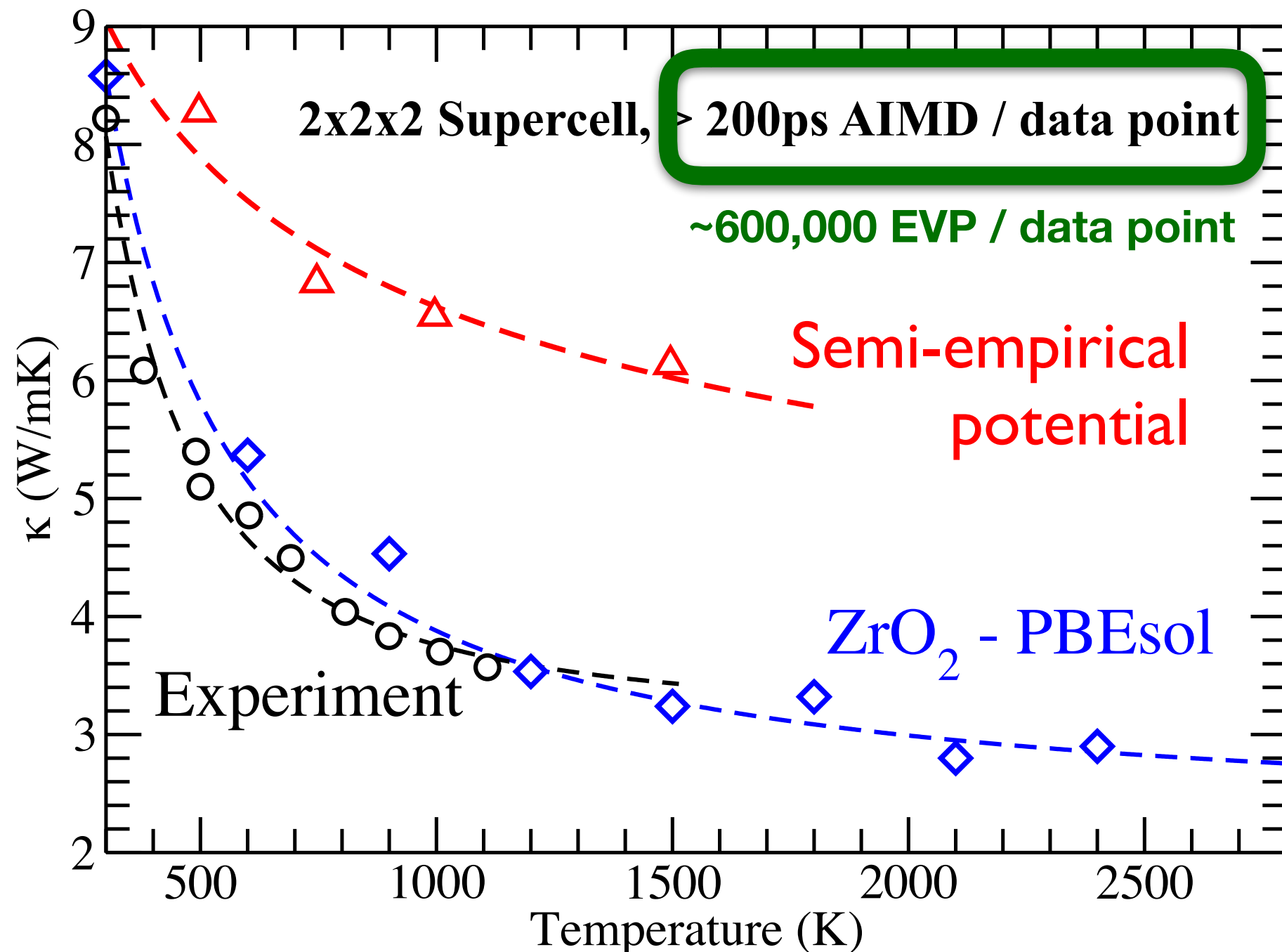
J.-F. Bisson *et al.*, *J. Am. Cer. Soc.* **83**, 1993 (2000).
G. E. Youngblood *et al.*, *J. Am. Cer. Soc.* **71**, 255 (1988).
S. Raghavan *et al.*, *Scripta Materialia* **39**, 1119 (1998).

Semi-empirical MD:

P. K. Schelling, and S. R. Phillpot,
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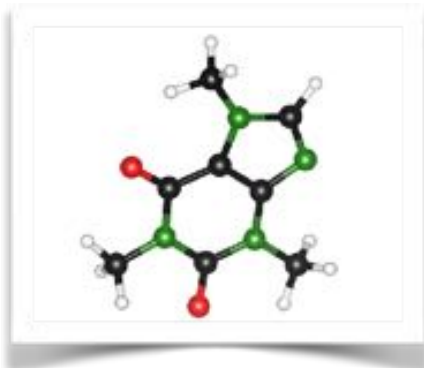
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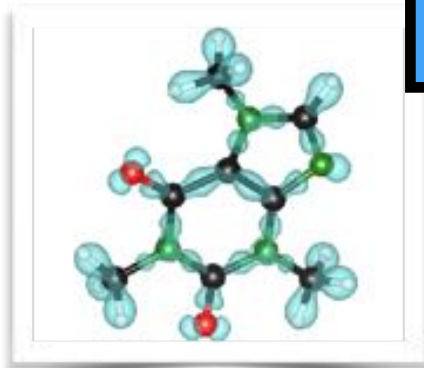
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Update Geometry



Geometry & Species



Electronic Structure Theory

Electronic Structure

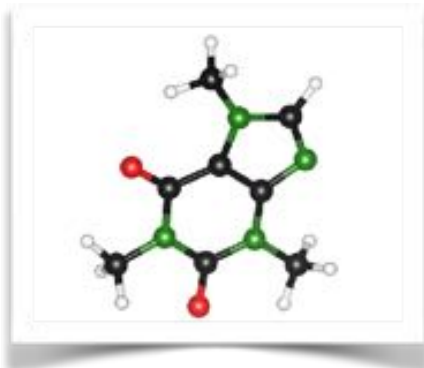
**Compute Energy E
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⇒ Materials' Properties

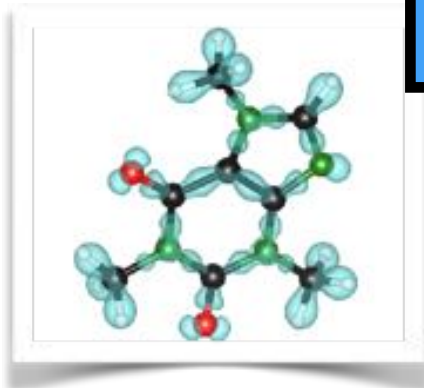
**A series of different,
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**A series of different,
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Electronic Structure Theory

Electronic Structure

**Compute Energy E
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**This Talk: How can this be exploited
within **ELPA** to accelerate applications.**

Overview:

Geometry Updates

Construct Matrix \underline{B}

Guess for $n_0(r)$

Construct $\underline{A}[n_i(r)]$

Solve Eigenvalue
Problem

Self-Consistency
achieved?

Compute other
quantities of
interest.

These are **several** self-consistency cycles.

*What can we do across many
electronic structure theory calculations?*

Hypothesis: For similar problems, similar numerical settings and code paths should be most efficient.

Typical Approach: Manually test different settings or choose (possibly automatically) by educated guess.

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ELPA's Autotuning Solution: Explicitly test different (combination of) settings and then choose the optimal one.
Possible settings include:

Code Paths:

ELPA 1
or
ELPA 2
solver?

**Optimized
Kernels:**

Generic,
AVX2, or
AVX512
kernel?

**Hybrid MPI/MP
Parallelization:**

Number of
threads / core

GPU offload:

Which routines
should make use
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This requires ELPA to “remember” settings and timings from earlier calls across one run.

Necessary Technology: *API Redefinition*






Old ELPA API

```
! Solve evp, return eigenvalues and eigenvectors
if(ph%elpa_solver == 2) then
    success = elpa_solve_evp_real_2stage_double(ph%n_good,ph%n_states_solve,&
        ham,bh%n_lrow,eval,vec,bh%n_lrow,bh%blk,bh%n_lcol,&
        ph%elpa_comm_row,ph%elpa_comm_col,bh%comm)
else
    success = elpa_solve_evp_real_1stage_double(ph%n_good,ph%n_states_solve,&
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endif
```

from els_i_elpa.f90 in ELSI

- **Traditional *Scalapack*-esque interface**
- **Stable and Here-to-Stay:**
All pre-2017 features are and will be accessible also in future
- **This includes all internal accelerations and kernels.**
- **New (optional) post-2017 features not accessible via the old API**

New ELPA API

- Object-oriented 
- Get/Set API 
- Mandatory and Optional Arguments are set separately 

- Actual ELPA call has simple syntax 
- ELPA Object survives iterations and cycles

```
! Create ELPA object
elpa => elpa_allocate()

! Set MANDATORY parameters describing the matrix and it's MPI distribution
call elpa%set("na", na, success)
call elpa%set("nev", nev, success)
call elpa%set("local_nrows", na_rows, success)
call elpa%set("local_ncols", na_cols, success)
call elpa%set("nblk", nblk, success)
call elpa%set("mpi_comm_parent", mpi_comm_world, success)
call elpa%set("process_row", my_prow, success)
call elpa%set("process_col", my_pcol, success)
success = elpa%setup()

! Set OPTIONAL run-time options
call elpa%set("solver", elpa_solver_2stage, success)

! Use ELPA
call elpa%eigenvectors(a, ev, z, success)
~
~
```

New ELPA API

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```

ELPA is able to store and exploit information across calls.

Example: Autotuning

- Usual setup →

- Attach Autotuning →

- Run your loops →

- Set optimal settings once identified →

```
! Setup ELPA using the new API
succes = elpa%setup()

! Autotuning setup
tune_state => elpa%autotune_setup(ELPA_AUTOTUNE_MEDIUM, ELPA_AUTOTUNE_DOMAIN_REAL, error)

! Loop of ELPA calls
do i=1, scf_cycles
  ! Autotuning still running?
  unfinished = elpa%autotune_step(tune_state)

  ! Use optimal setup once finished
  if (.not.(unfinished)) then
    call elpa%autotune_set_best(tune_state)
  endif

  ! ELPA call
  call elpa%eigenvectors(a, ev, z, error)
enddo
```

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```

Manual Settings or
Predefined Options

Example: Autotuning

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- Attach Autotuning →
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tune_state => elpa%autotune_setup(ELPA_AUTOTUNE_MEDIUM, ELPA_AUTOTUNE_DOMAIN_REAL, error)

! Loop of ELPA calls
do i=1, scf_cycles
  ! Autotuning still running?
  unfinished = elpa%autotune_step(tune_state)

  ! Use optimal setup once finished
  if (.not.(unfinished)) then
    call elpa%autotune_set_best(tune_state)
  endif

  ! ELPA call
  call elpa%eigenvectors(a, ev, z, error)
enddo
```

Manual Settings or
Predefined Options

Autotuning can be used during
production iterations.

Hypothesis: For similar problems, similar numerical settings and code paths should be most efficient.

Typical Approach: Manually test different settings or choose (possibly automatically) by educated guess.

ELPA's Autotuning Solution: Explicitly test different (combination of) settings and then choose the optimal one.
Possible settings include:

Code Paths:

ELPA 1
or
ELPA 2
solver?

ELPA_AUTOTUNE_FAST

**Optimized
Kernels:**

Generic,
AVX2, or
AVX512
kernel?

**Hybrid MPI/MP
Parallelization:**

Number of
threads / core

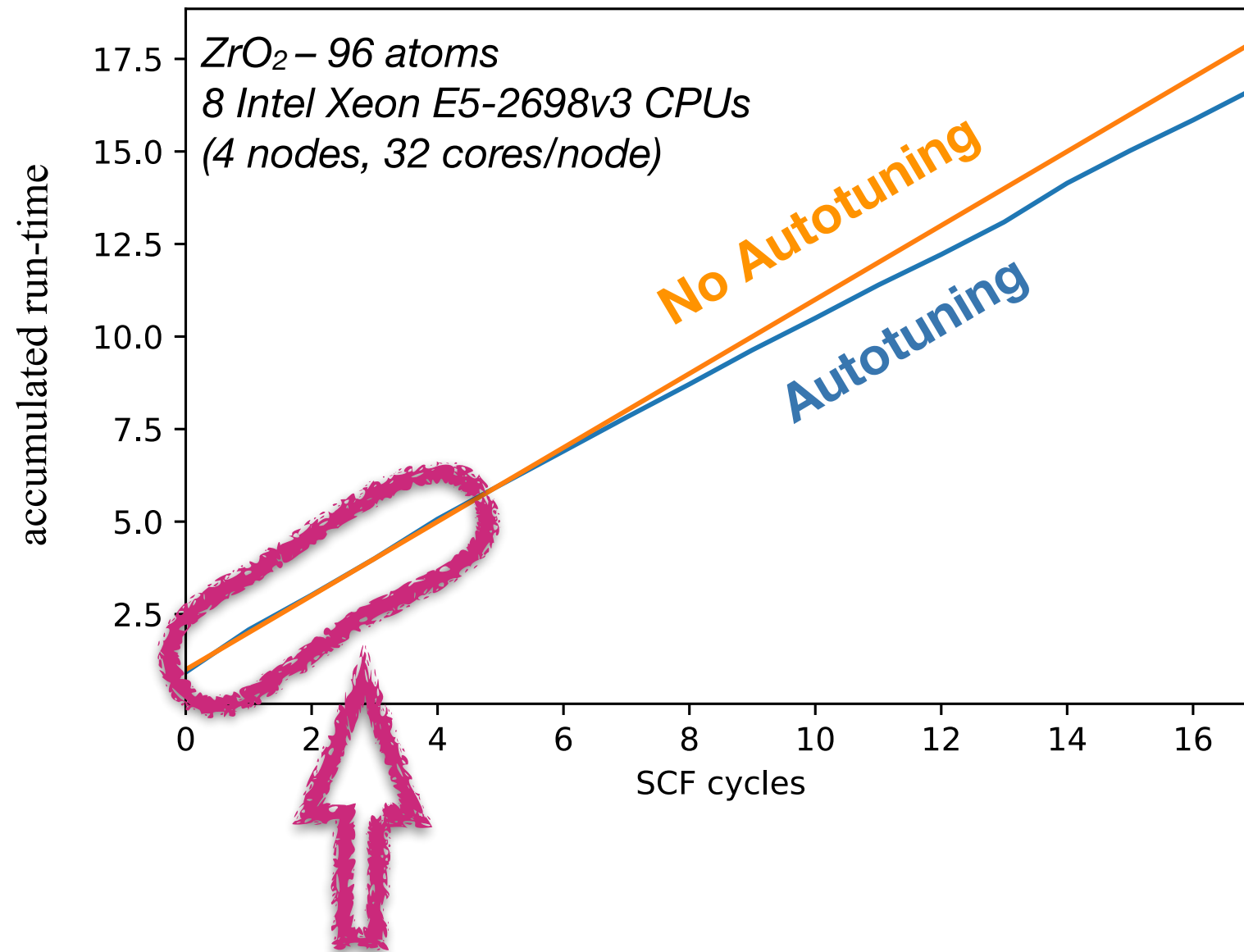
GPU offload:

Which routines
should make use
of GPUs?

Reasonable domain-specific presets such as **ELPA_AUTOTUNE_FAST**
available, more to come...

Autotuning with **ELPA_AUTOTUNE_FAST**

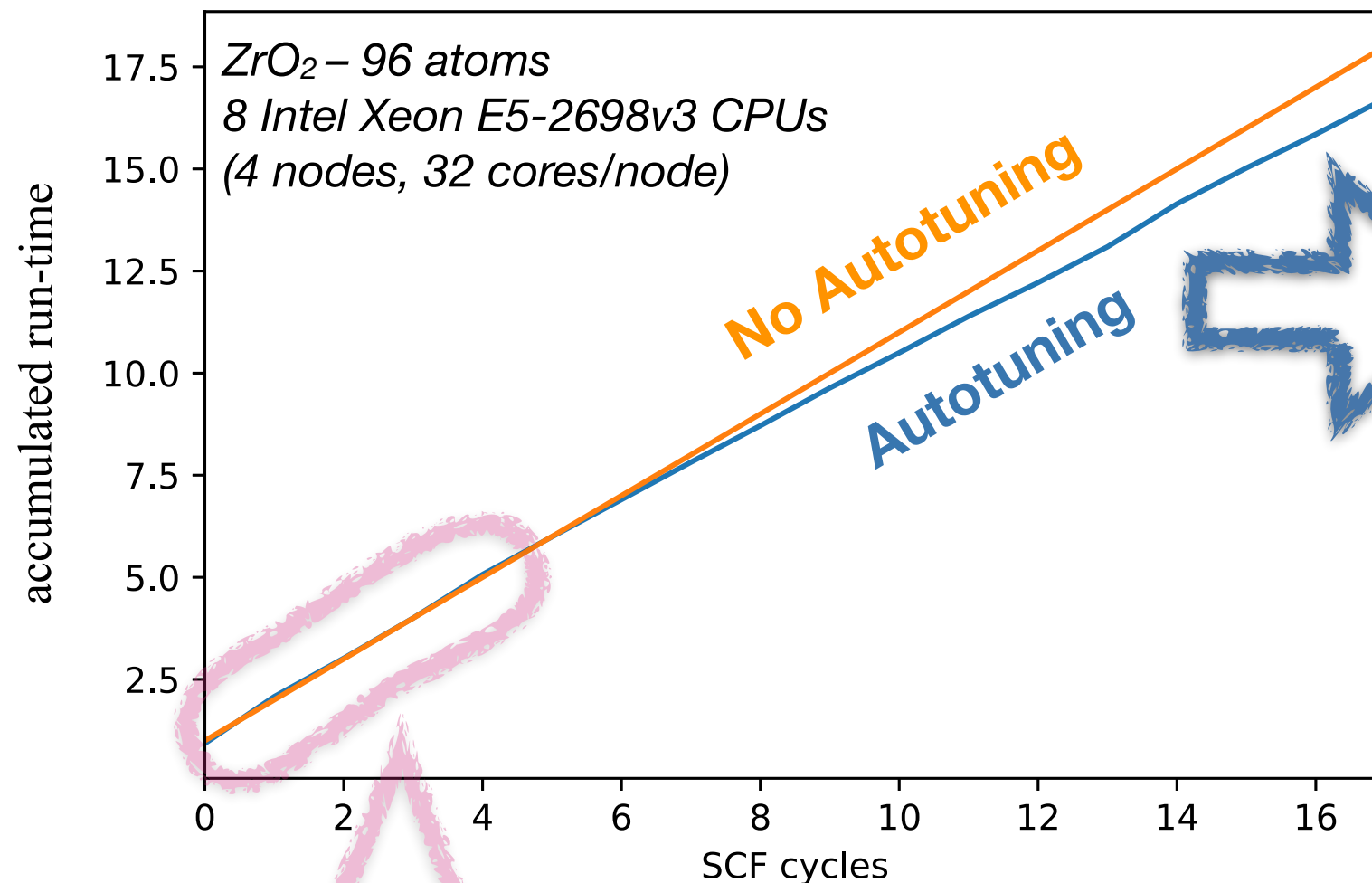
Accumulated Runtimes:



**Slight computational overhead
observed in the first couple of
iterations...**

Autotuning with **ELPA_AUTOTUNE_FAST**

Accumulated Runtimes:



Slight computational overhead
observed in the first couple of
iterations...

**Autotuning beneficial
in the long-run**

- **Autotuning** can already be beneficial in a single-run!
- Generally, **autotuning** can eventually leads to a speed-up between **15-20%** per SCF iteration.
- **Autotuning speed-up** retained across geometry changes (MD-ready!).

Overview:

Geometry Updates

Construct Matrix \underline{B}

Guess for $n_0(r)$

Construct $\underline{A}[n_i(r)]$

Solve Eigenvalue
Problem

Self-Consistency
achieved?

Compute other
quantities of
interest.

These are **several** self-consistency cycles.

⇒ (A) Exploit ELPA-Autotuning
for a series of calculations

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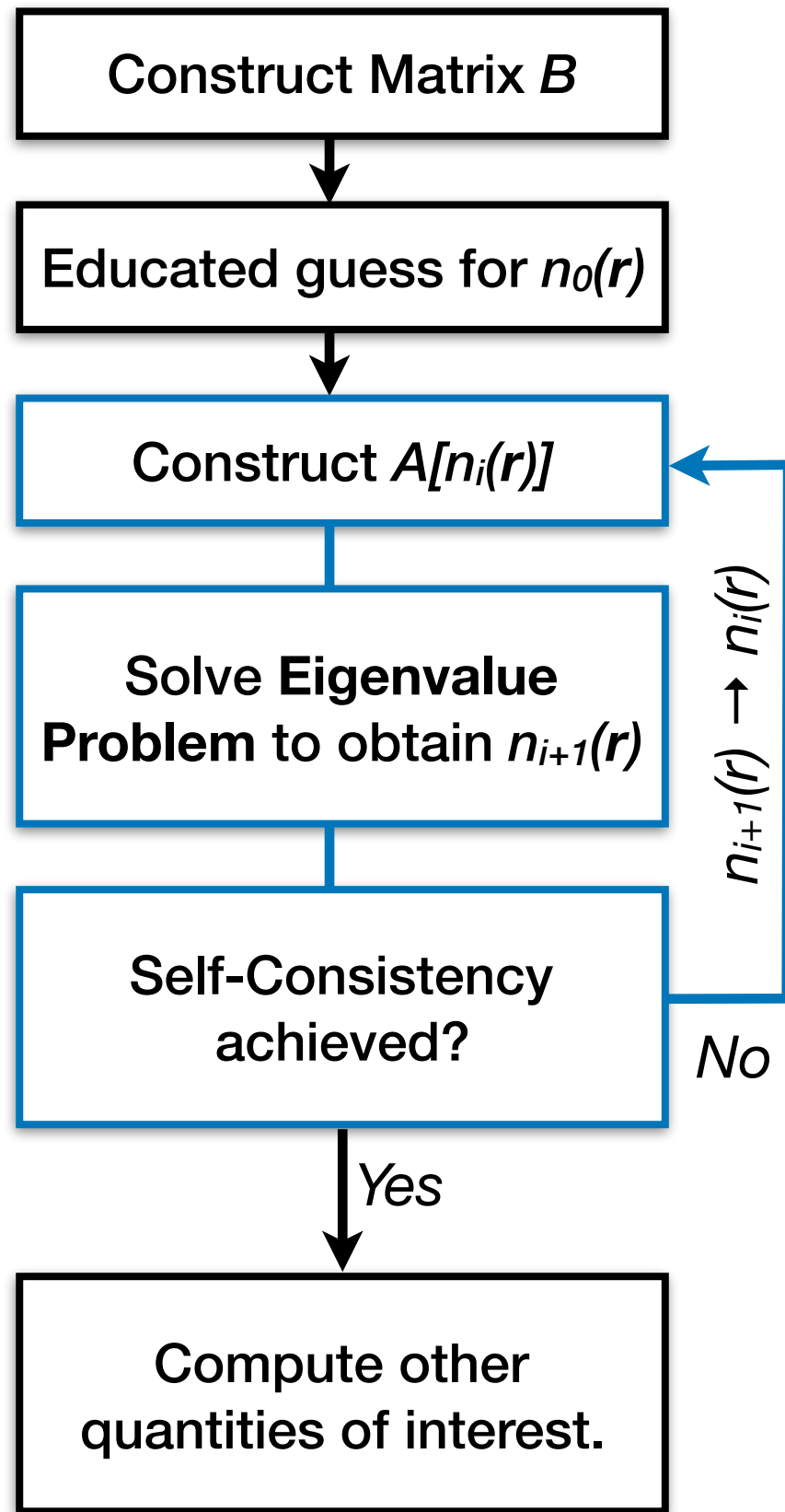
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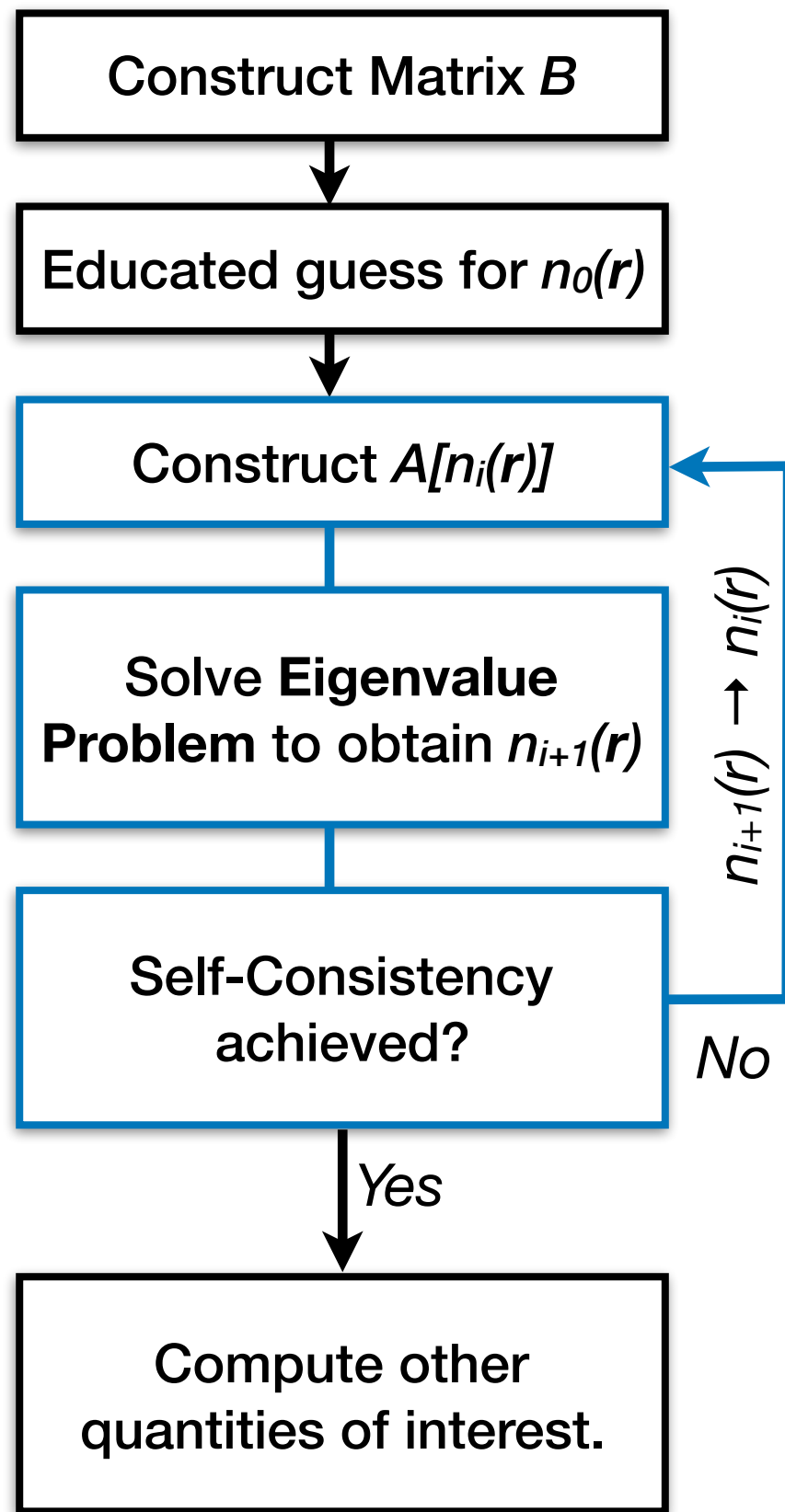
The Self-Consistency Cycle



Some Remarks:

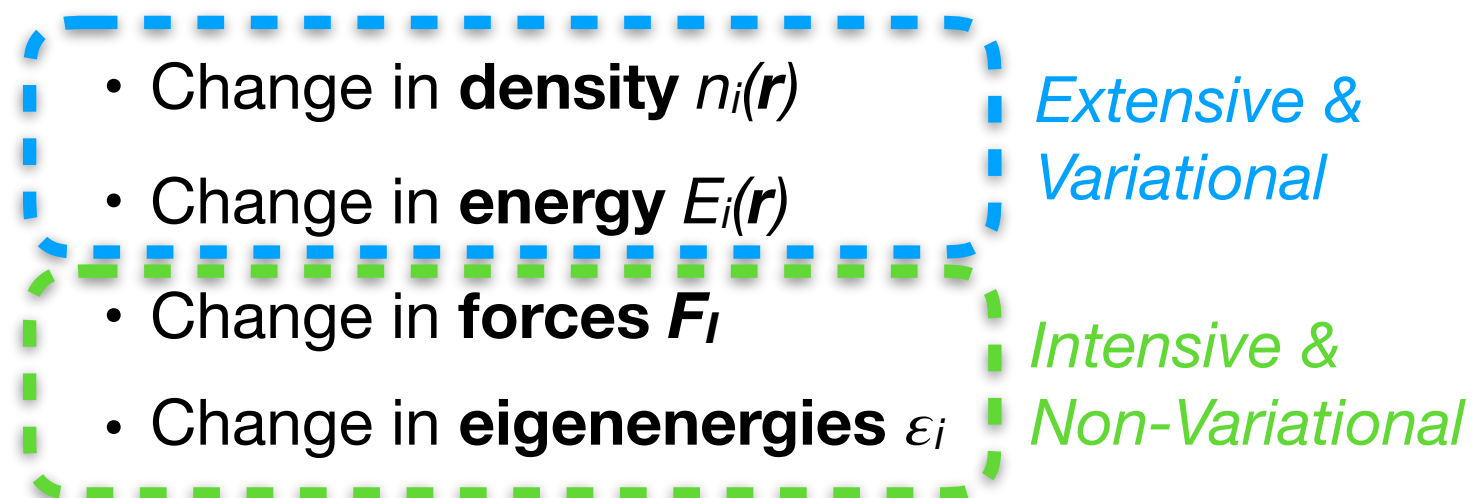
- **Typical number of iterations:** 10-100
- **Convergence accelerated by mixing schemes**
- **Convergence/Self-consistency monitored via:**
 - Change in **density** $n_i(r)$
 - Change in **energy** $E_i(r)$
 - Change in **forces** F_i
 - Change in **eigenenergies** ϵ_i

The Self-Consistency Cycle

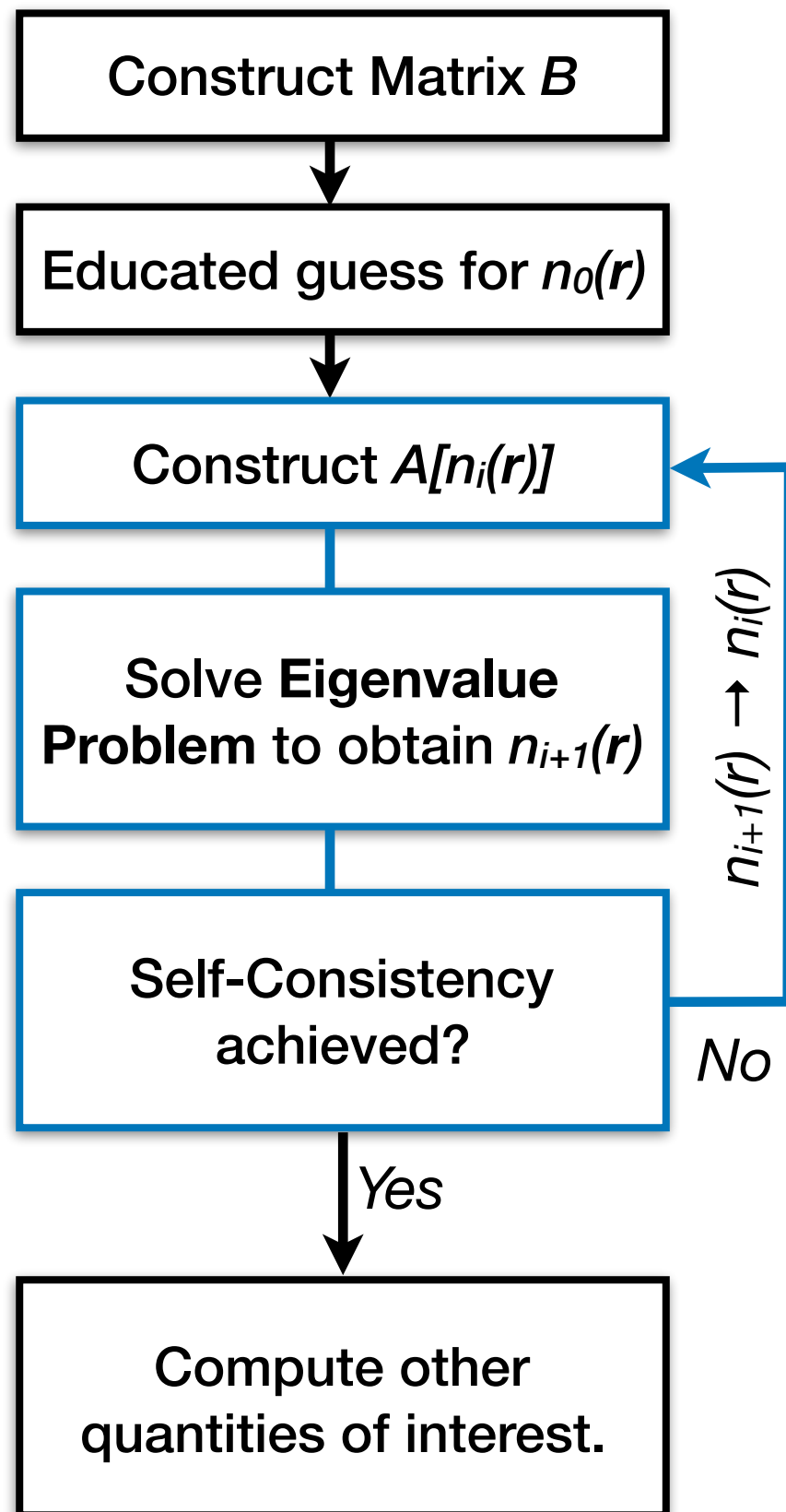


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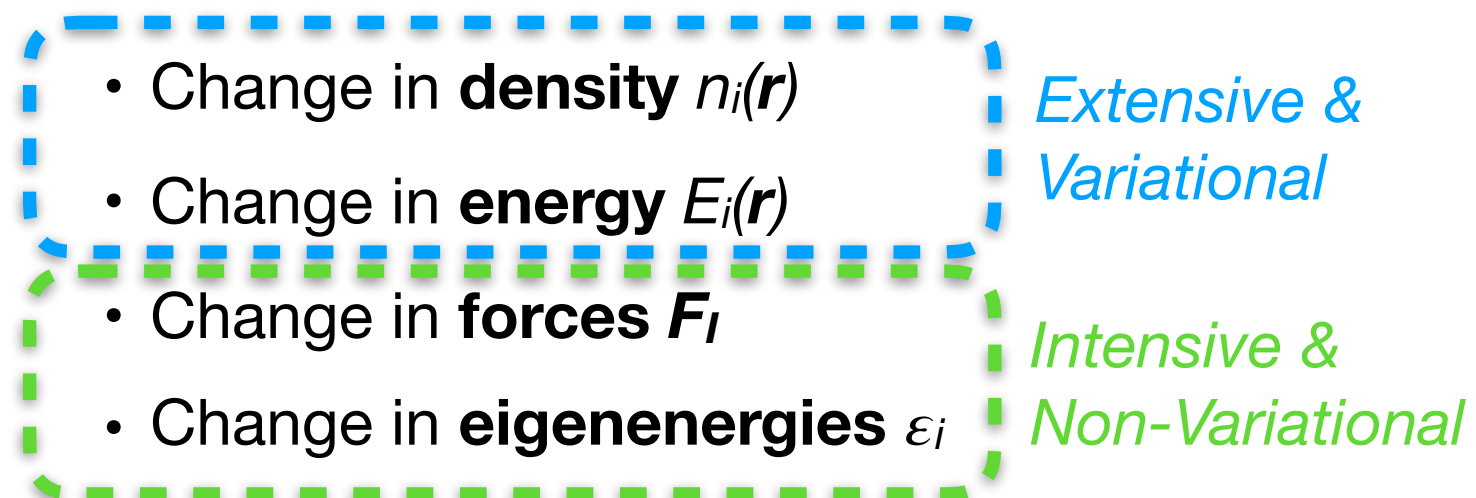


The Self-Consistency Cycle



Some Remarks:

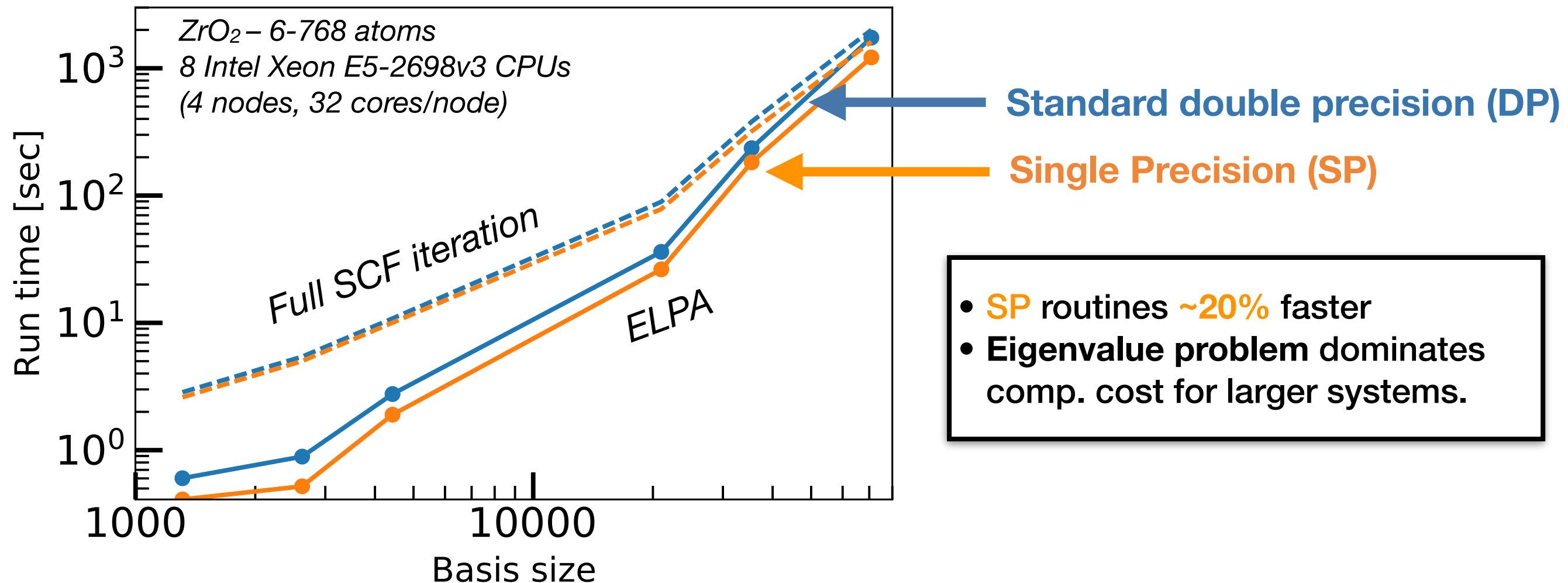
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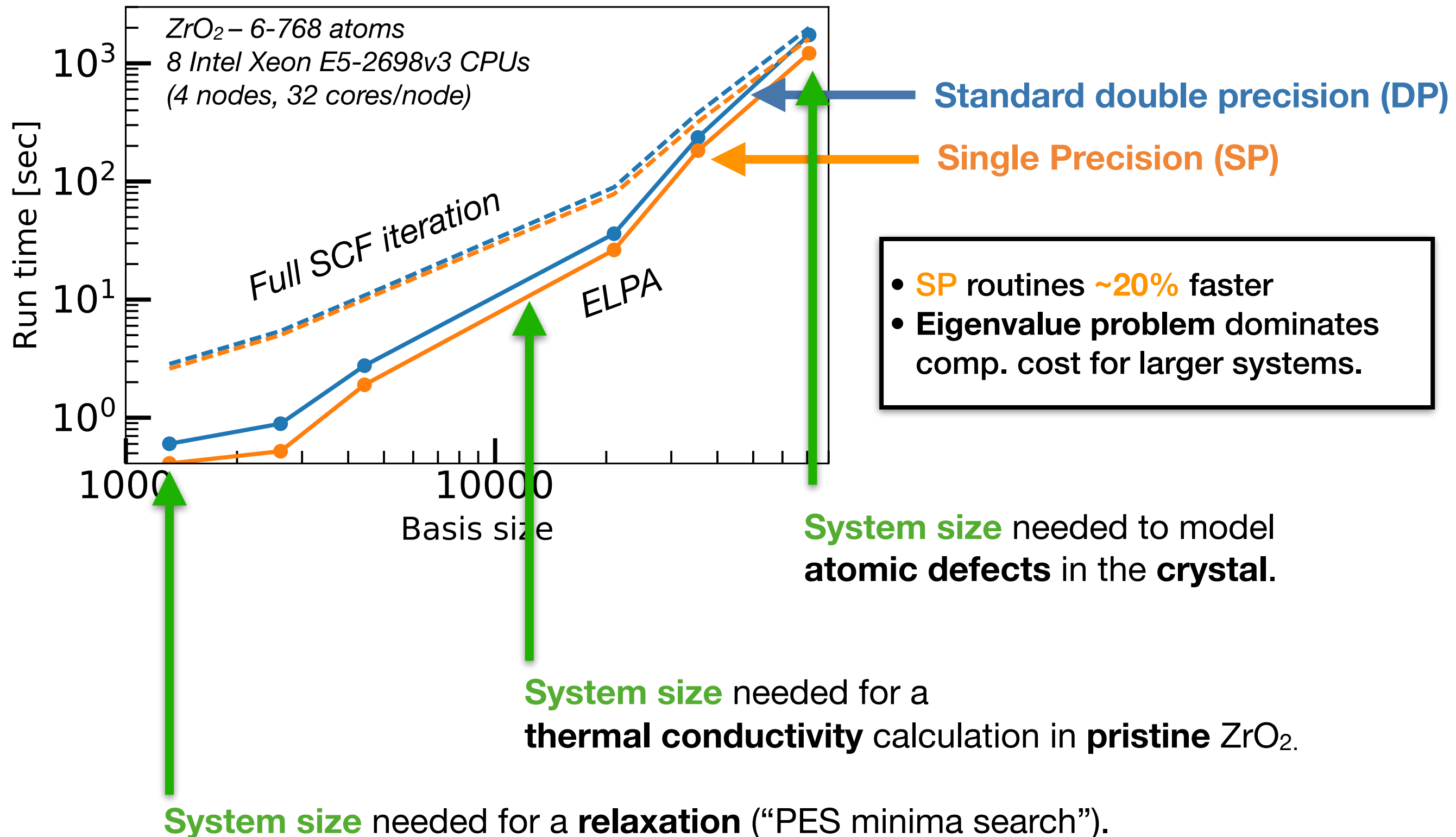
IDEA:

Use mixed precision to reduce computational cost
Perform the first self-consistency cycles with cheaper single precision routines.

Mixed Precision Calculations

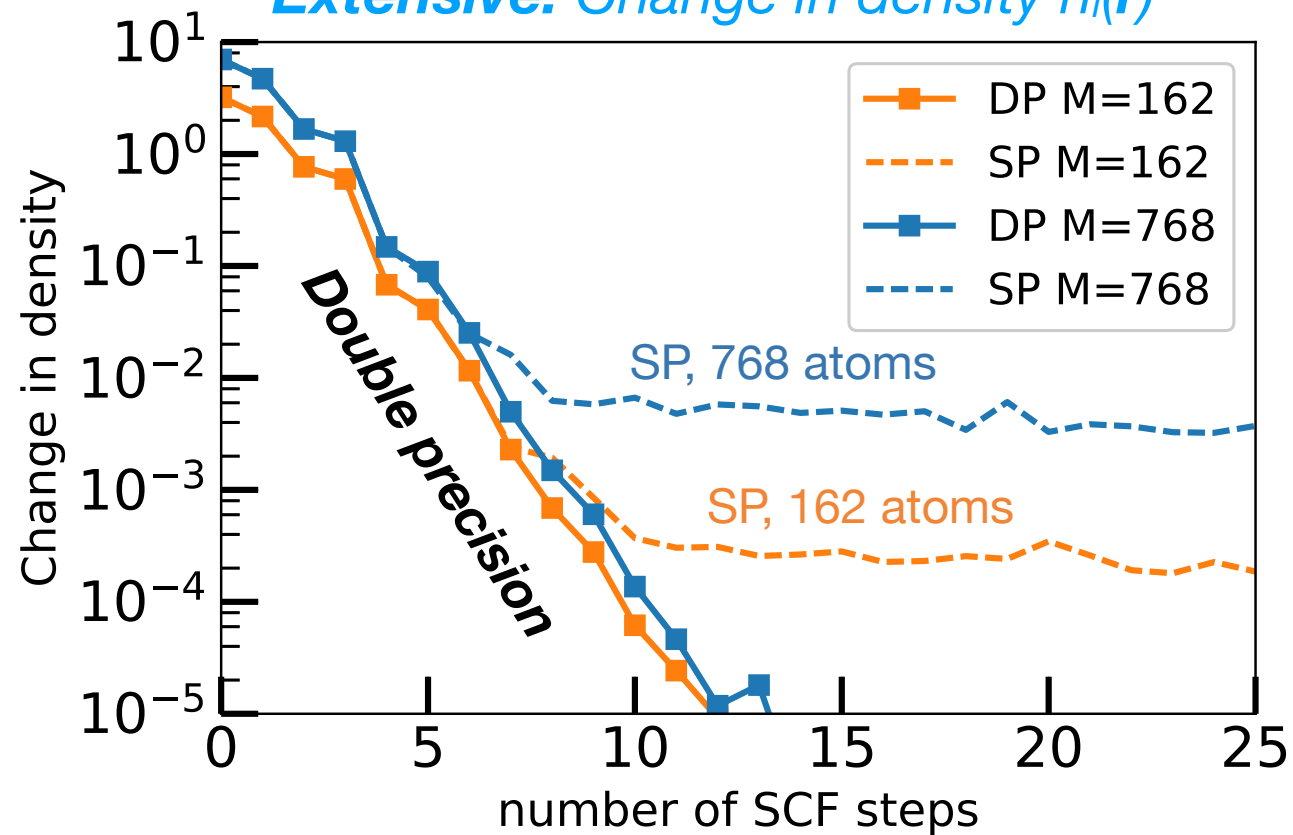


Mixed Precision Calculations



How far can we go?

Extensive: Change in density $n_i(r)$

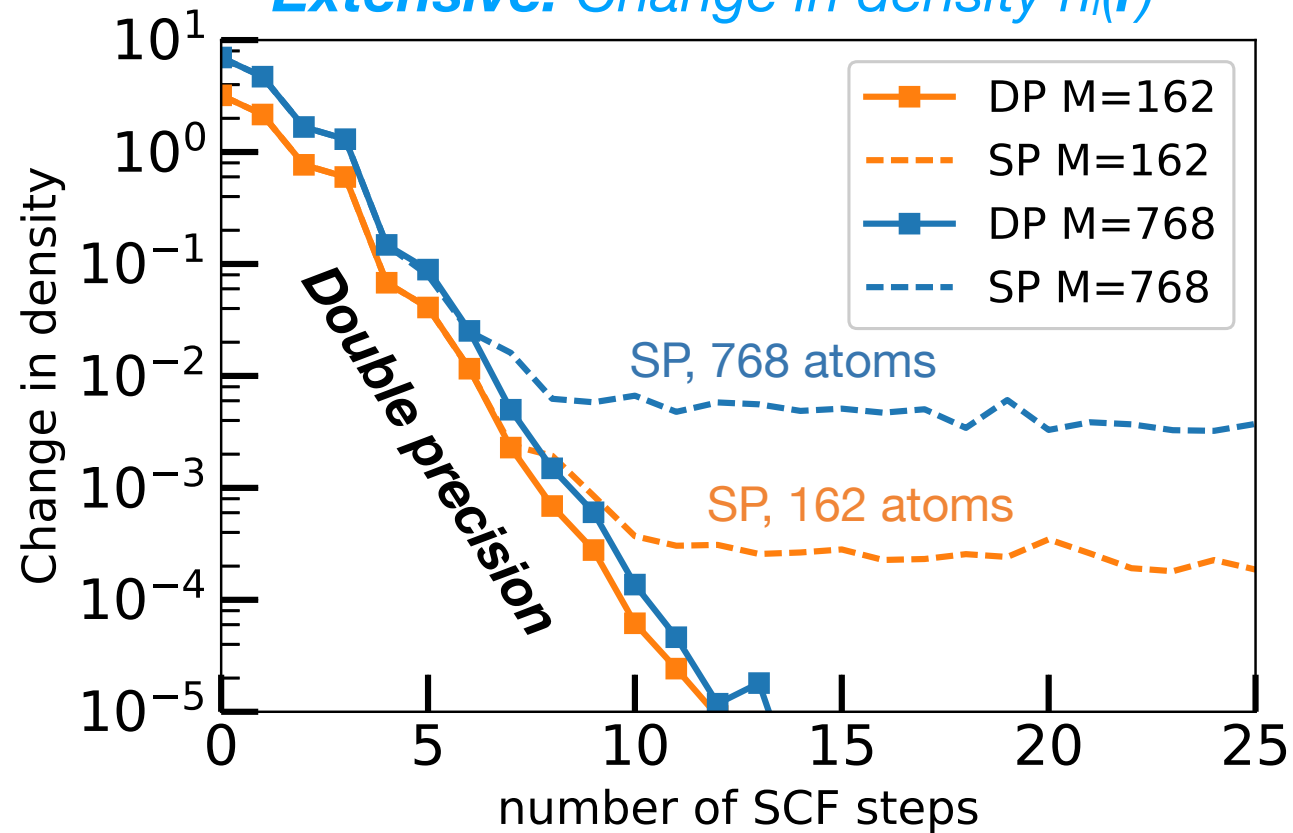


**Monitoring the convergence
of the self-consistency cycle**

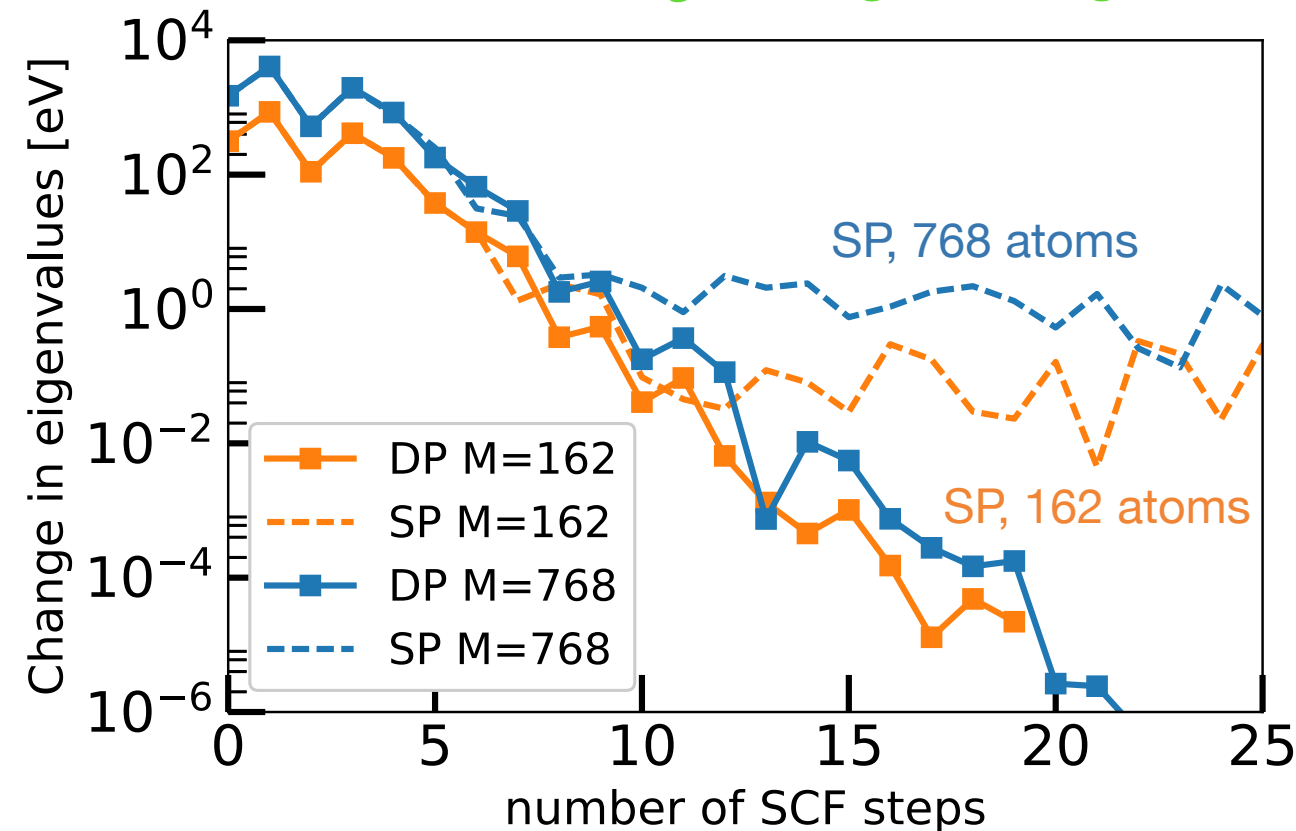
- **Single-Precision routines do not allow to reach convergence.**
- **“First” few iterations can be performed with single-precision without loss of accuracy.**
- **Break-down point of single-precision routines system-size-dependent.**

How far can we go?

Extensive: Change in density $n_i(r)$



Intensive: Change in eigenenergies ϵ_i

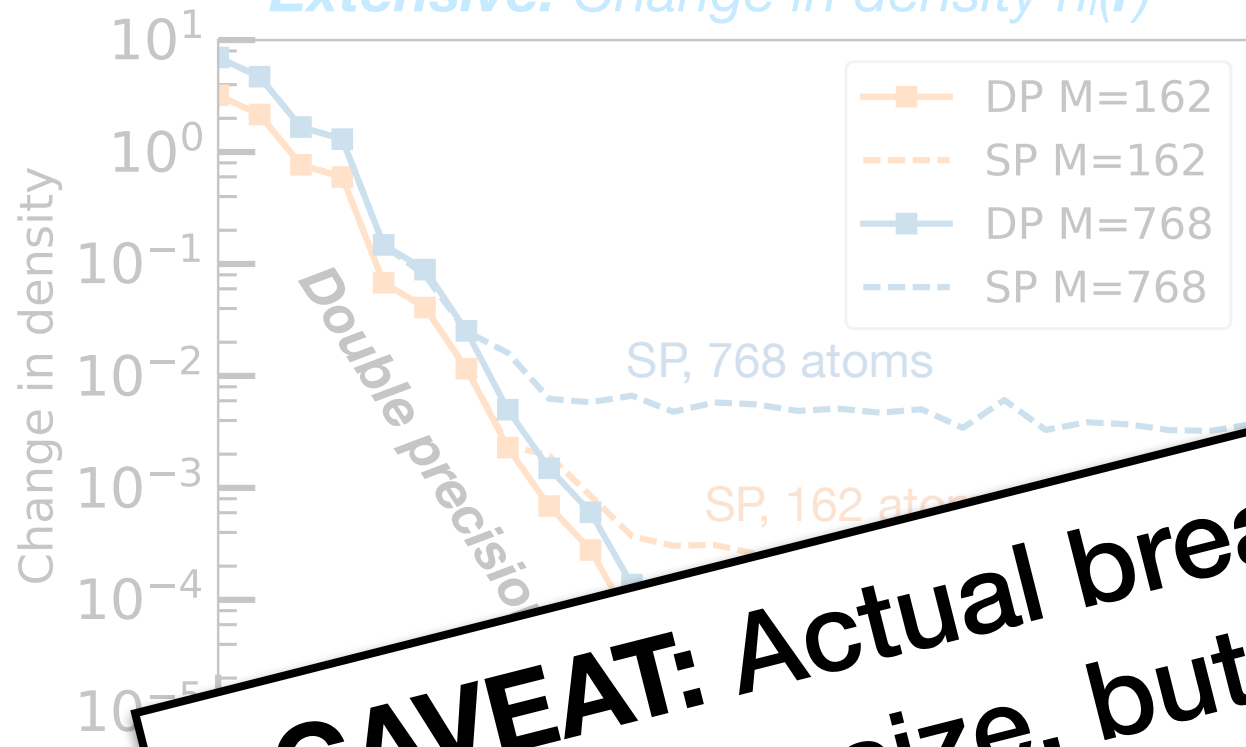


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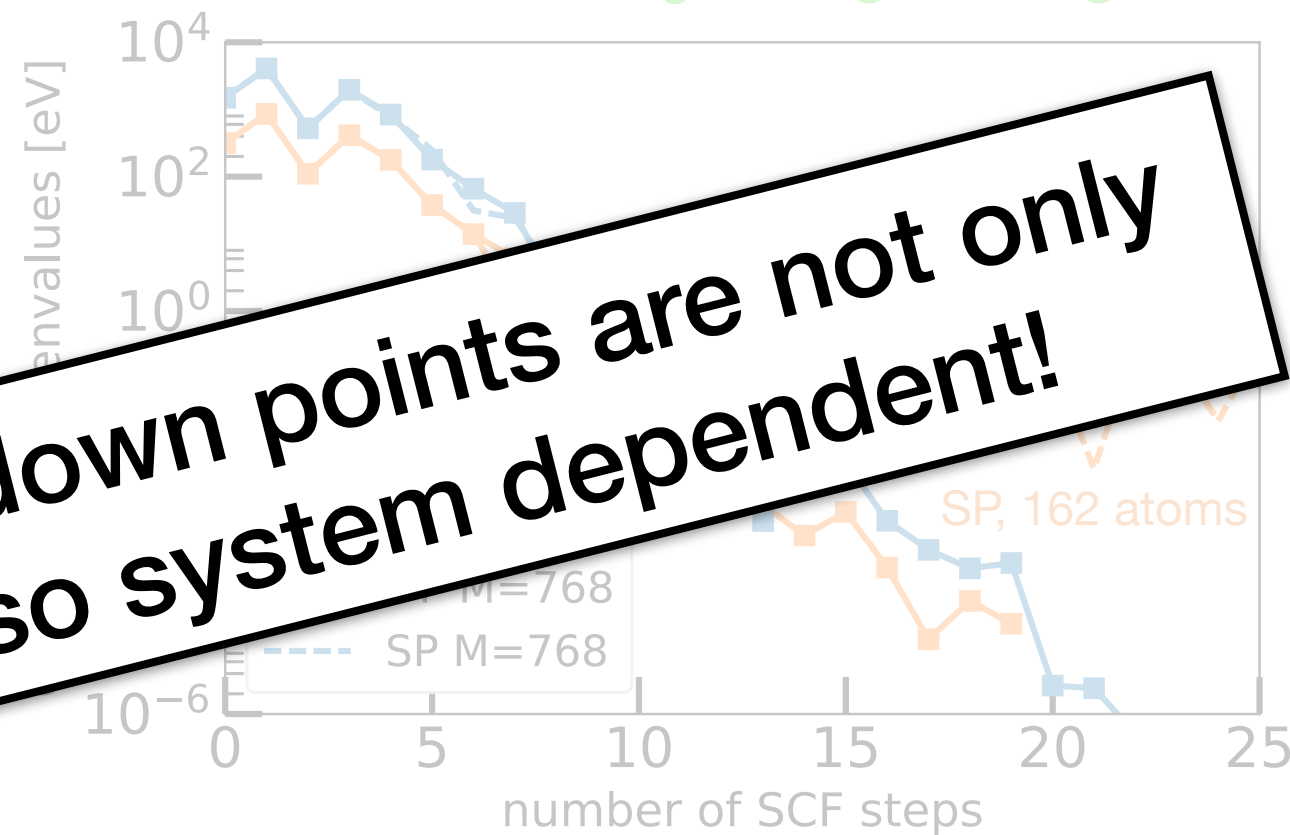
⇒ Intensive Quantities naturally less affected by system-size dependence.

How far can we go?

Extensive: Change in density $n_i(r)$



Intensive: Change in eigenenergies ϵ_i



CAVEAT: Actual breakdown points are not only system-size, but also system dependent!

- Single-Precision routines do not allow to reach convergence.
- “First” few iterations can be performed with single-precision without loss of accuracy.
- Break-down point of single-precision routines system-size-dependent.

⇒ Intensive Quantities naturally less affected by system-size dependence.

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Solve Eigenvalue Problem

Self-Consistency achieved?

Compute other quantities of interest.

These are **several** self-consistency cycles.

⇒ (A) Exploit ELPA-Autotuning for a series of calculations

This is **one** self-consistency cycle.
(Several Eigenvalue Problems)

⇒ (B) Exploit **Single/Double Precision** routines in ELPA-AEO for a series of Eigenvalue Problem

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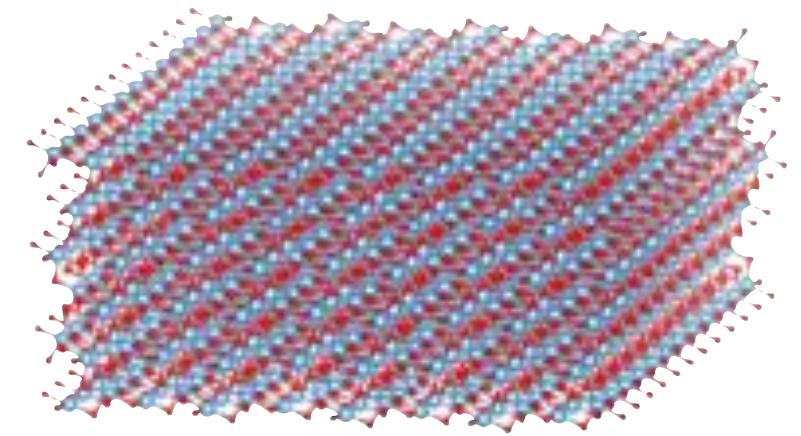
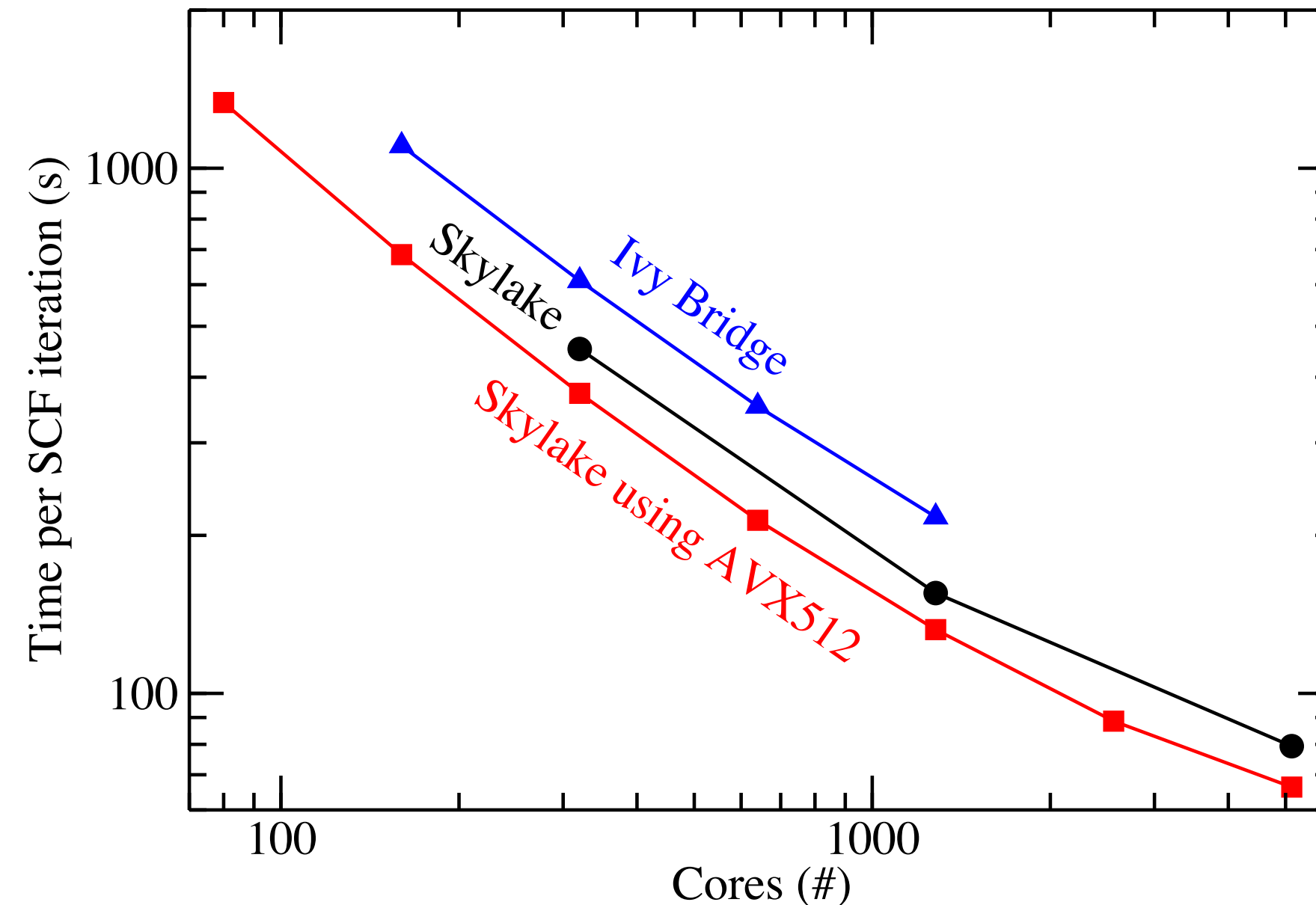
⇒ (B) Exploit Single/Double Precision routines in ELPA-AEO for a series of Eigenvalue Problem

This is **one** self-consistency iteration.
(One Eigenvalue Problem)

Accelerating One Iteration

Ivy Bridge: Hydra@MPCDF – 20 cores/node

Skylake: Cobra@MPCDF – 40 cores/node



TiO₂ slab/surface with
3,500 atoms and
100 Å vacuum

⇒ **Optimizations in ELPA**

directly translate into an **application speed-up**.

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⇒ (C) Exploit optimizations in ELPA-AEO for single Eigenvalue Problem

Acknowledgments



**Danilo
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FHI**

*(now at some
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und Forschung



Volker Blum

Victor Yu



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**Matthias
Schiffer**



**All features discussed in this talk,
including the new API
are available and usable
in ELSI.**

The ELSI

<http://>



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MAX PLANCK
COMPUTING &
DATA FACILITY



TUM



TUM



Bundesministerium
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und Forschung



Volker Blum



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(One Eigenvalue Problem)

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